

Engineered surfaces: from concept to applications

Shah Nawaz Burokur (Université Paris Nanterre)

Télécom Paris, Nov. 20 2024

Brief History of metamaterials / metasurfaces for wavefronts control

Left-handed medium
Negative refraction



Veselago

1964

Realized
 $-\epsilon, -\mu$



Pendry

1996 1999

Experimental verification
of negative refraction



Smith

2001

Transformation optics
Invisibility cloak



Pendry / Smith

2006

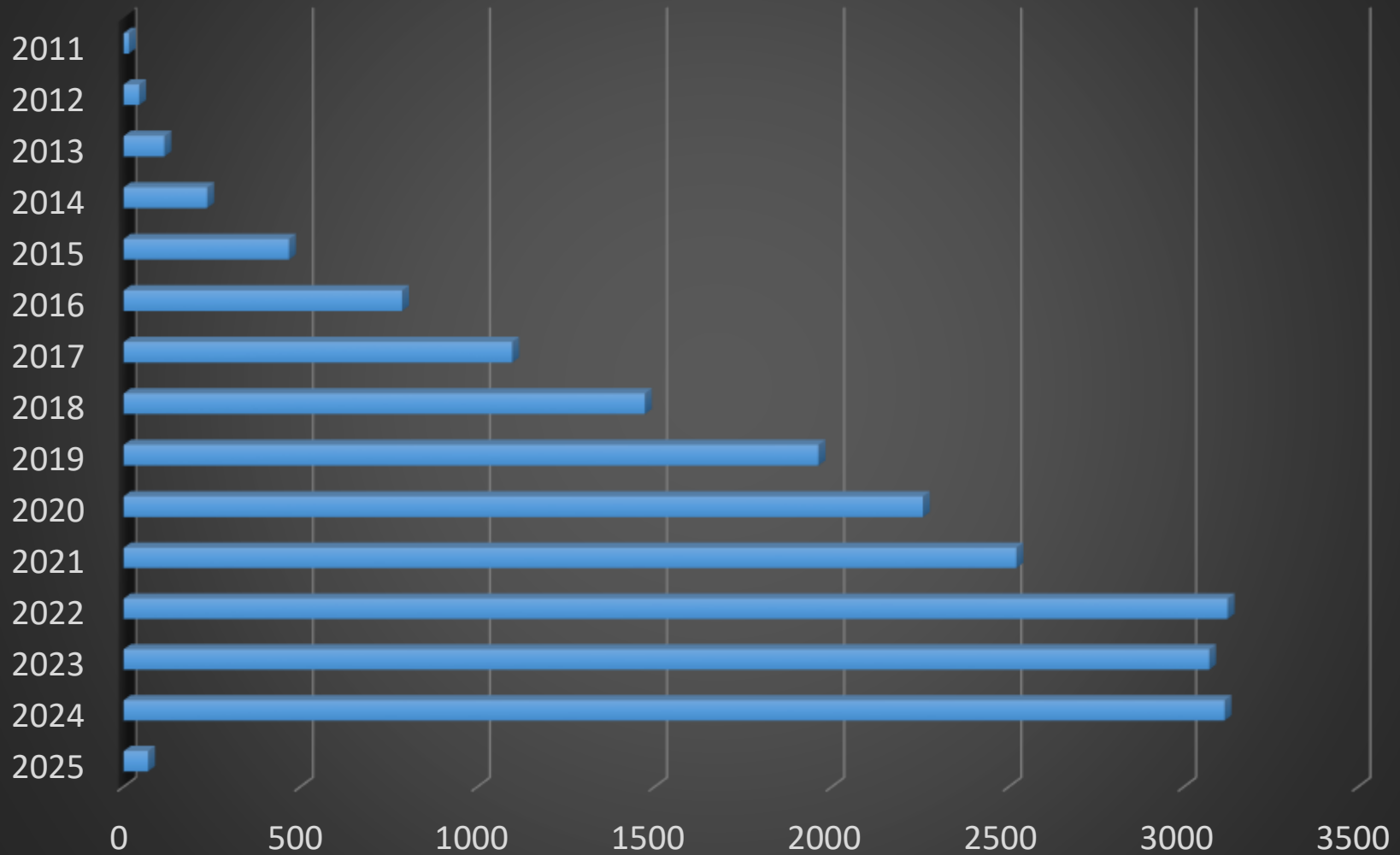
Metasurface
Generalized Snell's law



Capasso

2011

Publications on Metasurfaces (ISI WoS)



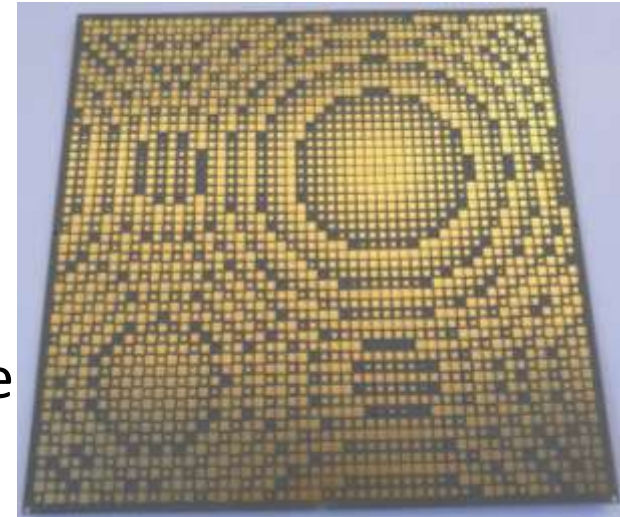


Outlines

1. Metasurface definition
2. Metasurface classification
3. Applications
4. Actual trends
5. Summary

1. Metasurface definition

- Two-dimensional arrays of subwavelength-scale artificial elements, arranged in a specific pattern to manipulate the propagation of light at subwavelength scales
- Geometry, size and arrangement of meta-atoms → Tailor EM response
- Planar structures that can be fabricated on flat substrates, making them compatible with existing fabrication techniques
- Metasurfaces can control the phase, amplitude, and polarization of incident light across a planar surface, enabling unprecedented control over the wavefront of light

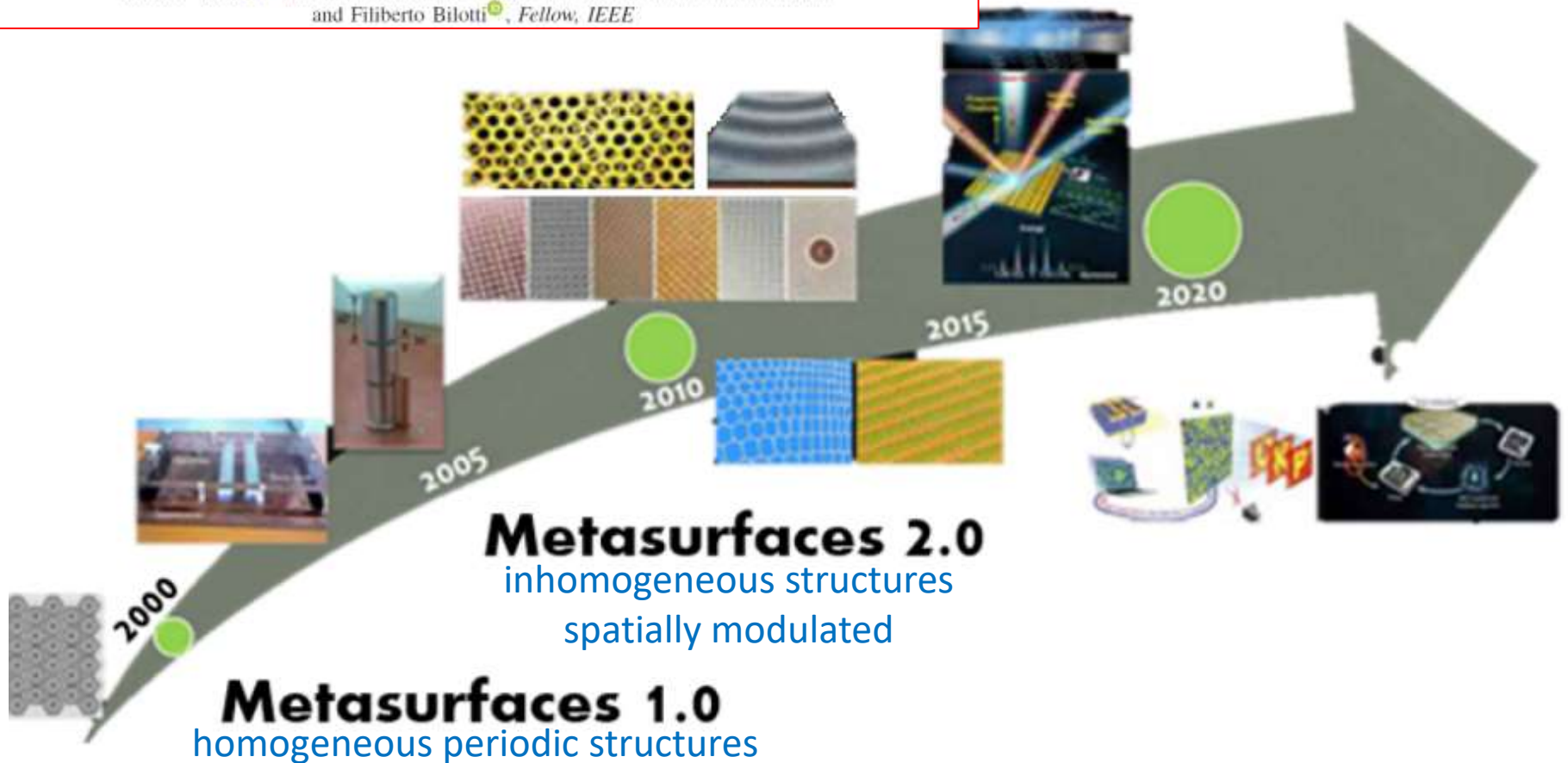


1. Metasurface definition: Design evolution

Metasurfaces 3.0: A New Paradigm for Enabling Smart Electromagnetic Environments

Mirko Barbuto¹, Senior Member, IEEE, Zahra Hamzavi-Zarghani², Michela Longhi,
Alessio Monti³, Senior Member, IEEE, Davide Ramaccia⁴, Senior Member, IEEE,
Stefano Vellucci⁵, Member, IEEE, Alessandro Toscano, Senior Member, IEEE,
and Filiberto Bilotti⁶, Fellow, IEEE

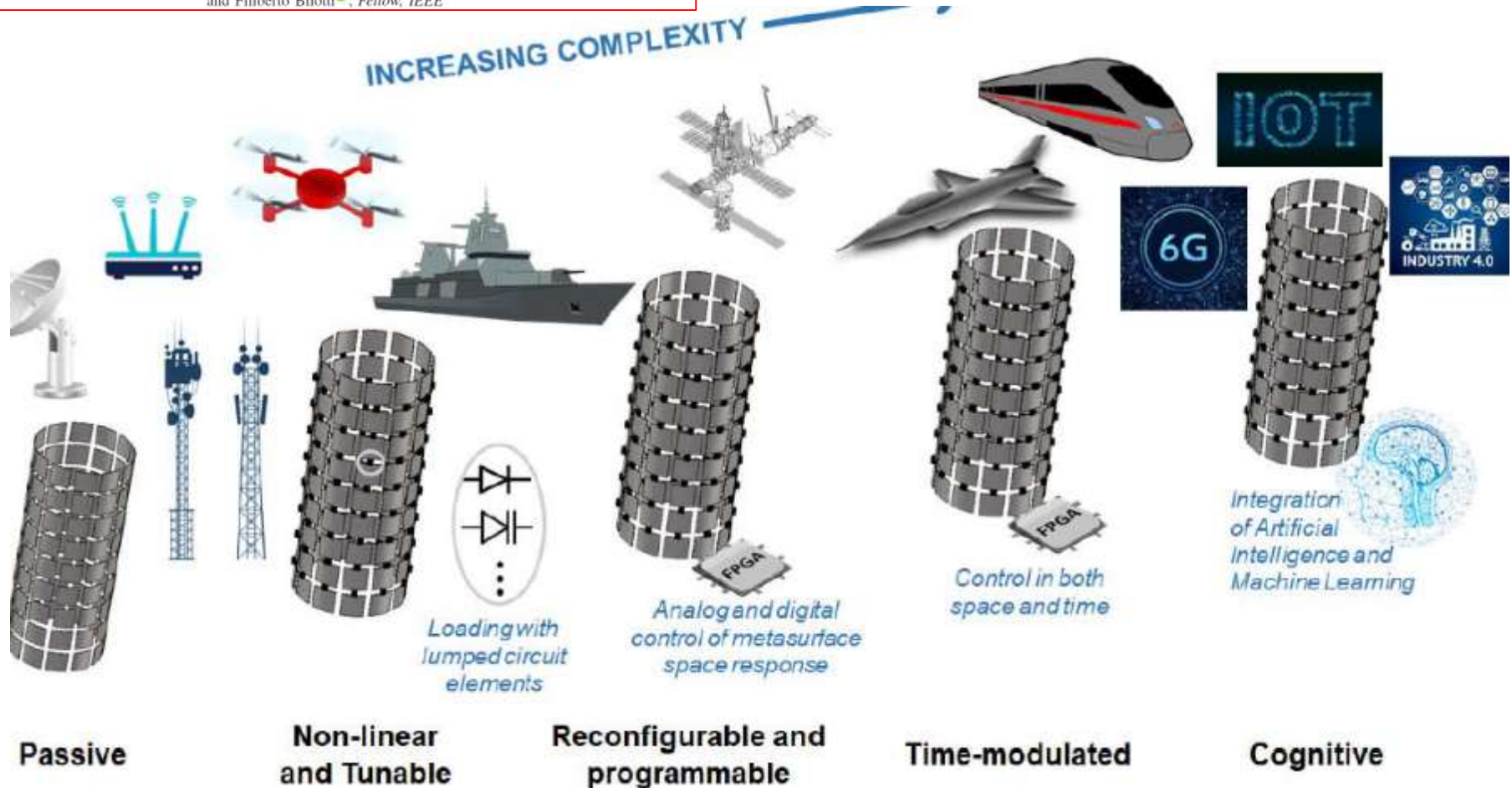
(in)homogeneous structures
temporally modulated
Metasurfaces 3.0



1. Metasurface definition: Design evolution

Metasurfaces 3.0: A New Paradigm for Enabling Smart Electromagnetic Environments

Mirko Barbuto¹, Senior Member, IEEE, Zahra Hamzavi-Zarghani², Michela Longhi,
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and Filiberto Bilotti⁶, Fellow, IEEE



2. Metasurface classification

3 main categories

- Dense metasurfaces
- Metagratings
- Sparse metasurfaces

Dense Metasurfaces

- Continuous impedance sheets, i.e., they require dense distribution of unit cells
- Designed by means of local periodic approximation (LPA)
- So far, metasurfaces present narrow-band performances

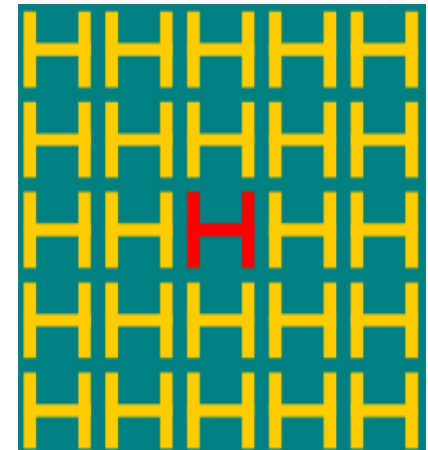
characteristic of the whole array:

$$Z_{in} = Z_0 \frac{1+S_{11}}{1-S_{11}}$$

Non-uniform array



Uniform array

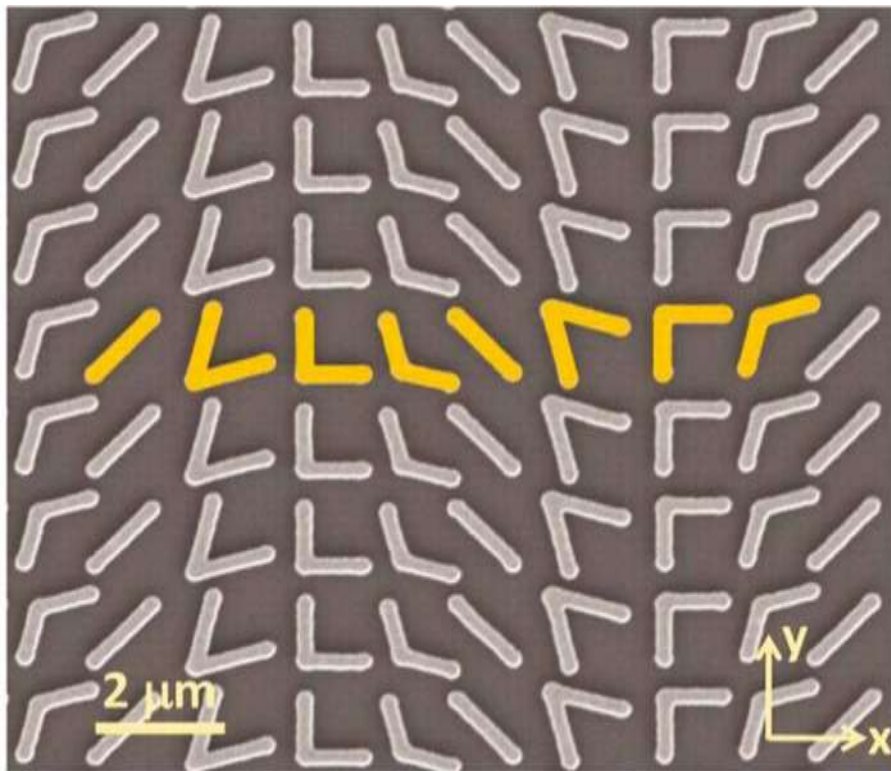


Dense Metasurfaces

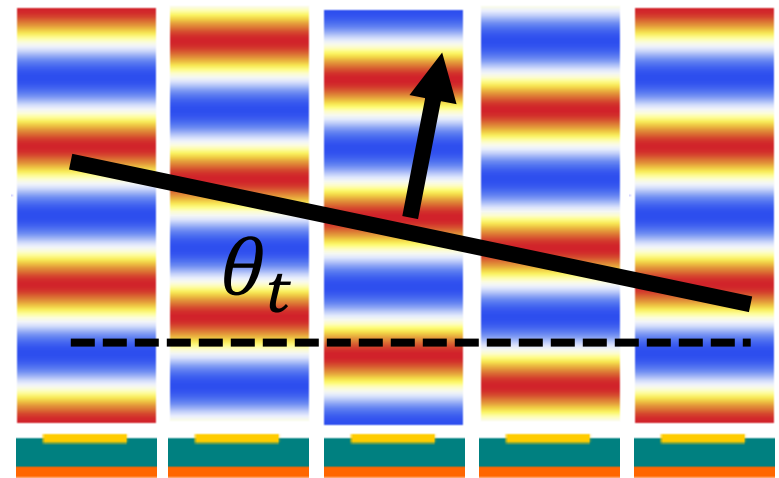
Light Propagation with Phase Discontinuities: Generalized Laws of Reflection and Refraction

NANFANG YU, PATRICE GENEVET, MIKHAIL A. KATS, FRANCESCO AIETA, JEAN-PHILIPPE TETIENNE, FEDERICO CAPASSO, AND ZENO GABURRO

SCIENCE • 1 Sep 2011 • Vol 334, Issue 6054 • pp. 333-337 • DOI: 10.1126/science.1210713

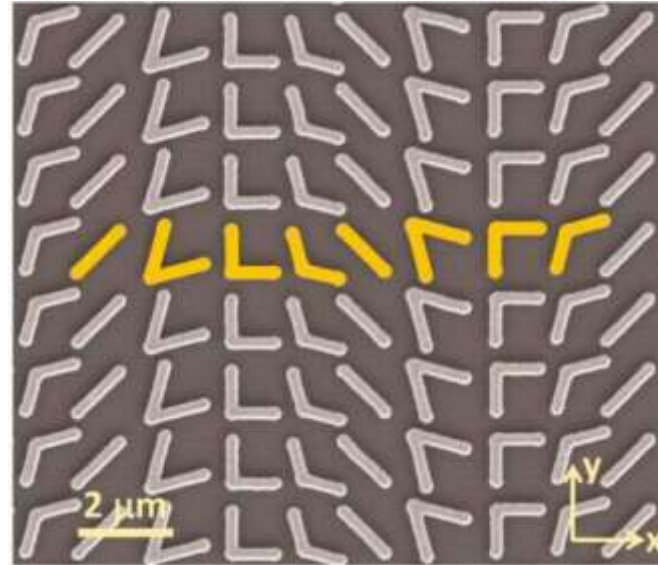


$$\sin[\theta_t]n_t - \sin[\theta_i]n_i = \frac{\lambda_0}{2\pi} \frac{d\Phi(x)}{dx}$$



Dense Metasurfaces

Phase-gradient
metasurfaces



Performance is
fundamentally
limited: **increased
side-lobes level**

Many elements: **high
absorption because
of many tunable
elements**

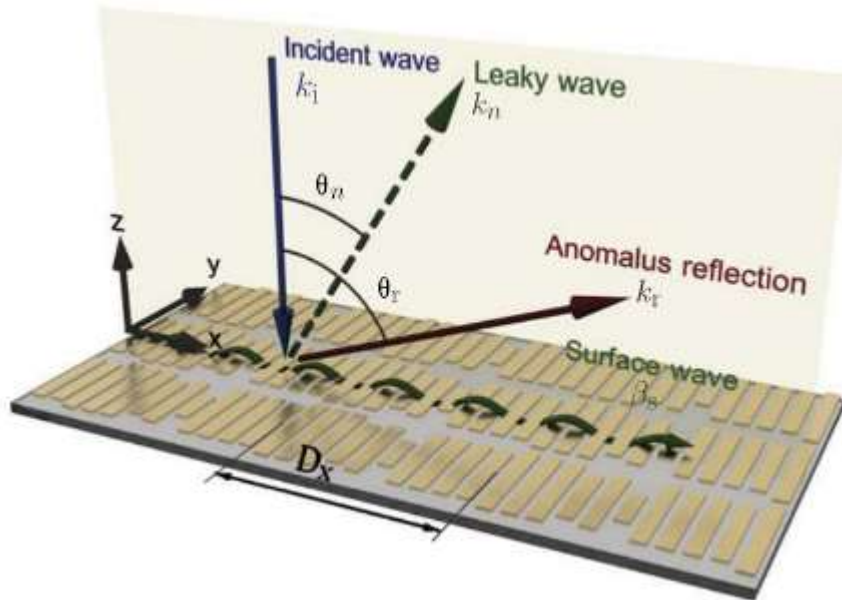
Dense Metasurfaces

From the generalized reflection law to the realization of perfect anomalous reflectors

ANA DÍAZ-RUBIO , VIKTAR S. ASADCHY, AMR ELSAKKA, AND SERGEI A. TRETYAKOV [Authors Info & Affiliations](#)

SCIENCE ADVANCES • 11 Aug 2017 • Vol 3, Issue 8 • DOI: 10.1126/sciadv.1602714

- Concept: strong non-locality



- Drawbacks

Complicated design procedure strongly relying on 3D full-wave optimization

Dense arrangement of elements

engineering the interaction between distant parts by SW

Dense Metasurfaces: Huygens' metasurfaces

Selected for a **Viewpoint** in *Physics*
 PHYSICAL REVIEW LETTERS

week ending
 10 MAY 2013

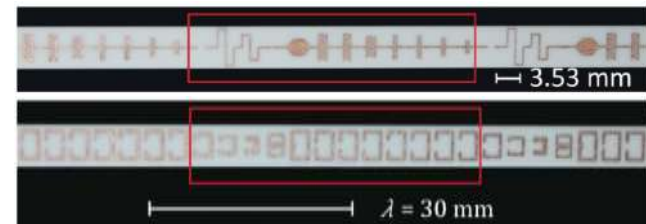
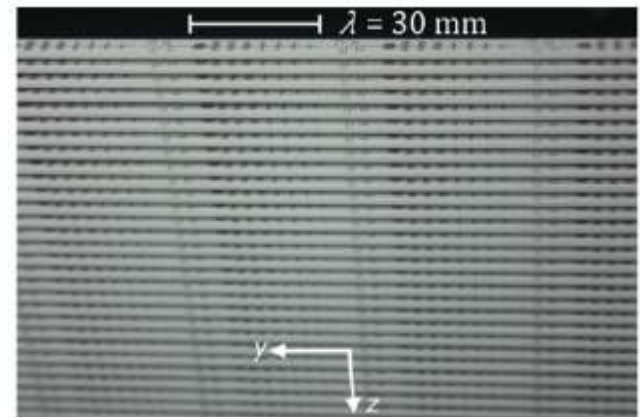
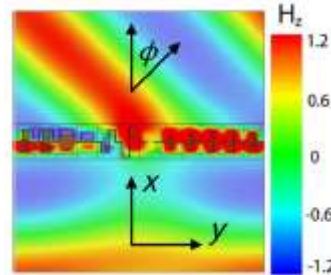
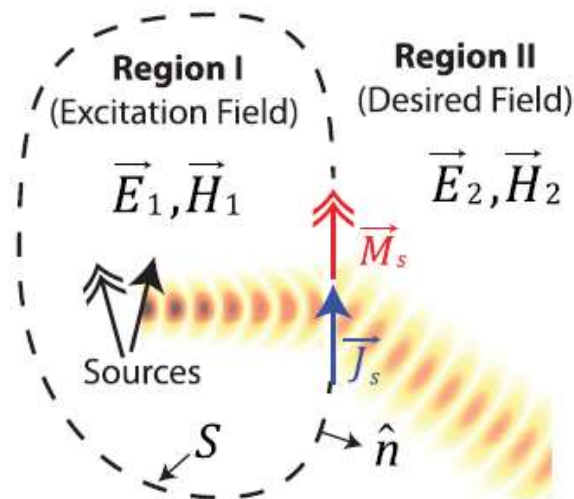


Metamaterial Huygens' Surfaces: Tailoring Wave Fronts with Reflectionless Sheets

Carl Pfeiffer and Anthony Grbic*

- Huygens' principle:

each point on a wavefront acts as a secondary source of outgoing waves



$$\vec{J}_s = \hat{n} \times (\vec{H}_2 - \vec{H}_1),$$

$$\vec{M}_s = -\hat{n} \times (\vec{E}_2 - \vec{E}_1)$$

$$Y_{es} = \frac{2(1 - T - R)}{\eta(1 + T + R)},$$

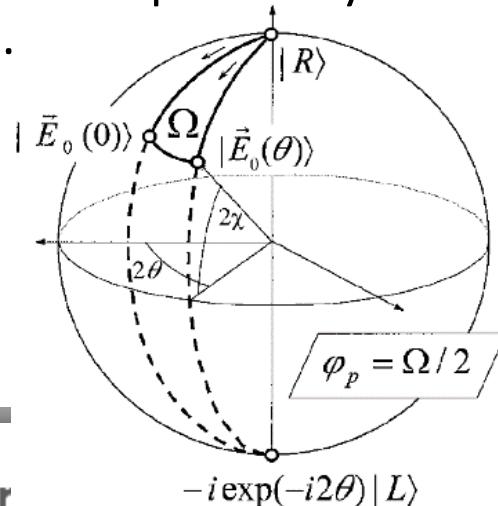
$$Z_{ms} = \frac{2\eta(1 - T + R)}{(1 + T - R)}$$

Space-variant Pancharatnam–Berry phase optical elements with computer-generated subwavelength gratings

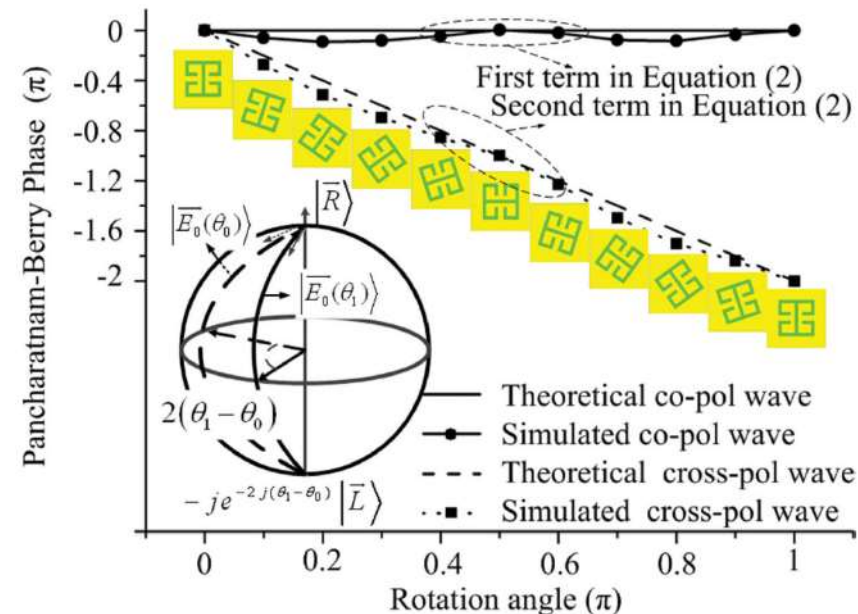
Ze'ev Bomzon, Gabriel Biener, Vladimir Kleiner, and Erez Hasman

• Pancharatnam-Berry phase:

geometric phase associated with the polarization of light. When the polarization of a beam traverses a closed loop on the Poincaré sphere, the final state differs from the initial one by a phase factor equal to half of the Ω area, encompassed by the loop on the sphere.



A rotation of θ will introduce a phase shift of 2θ



Dense Metasurfaces: Coding metasurfaces

Light: Science & Applications (2014) 3, e218; doi:10.1038/lisa.2014.99

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www.nature.com/lisa



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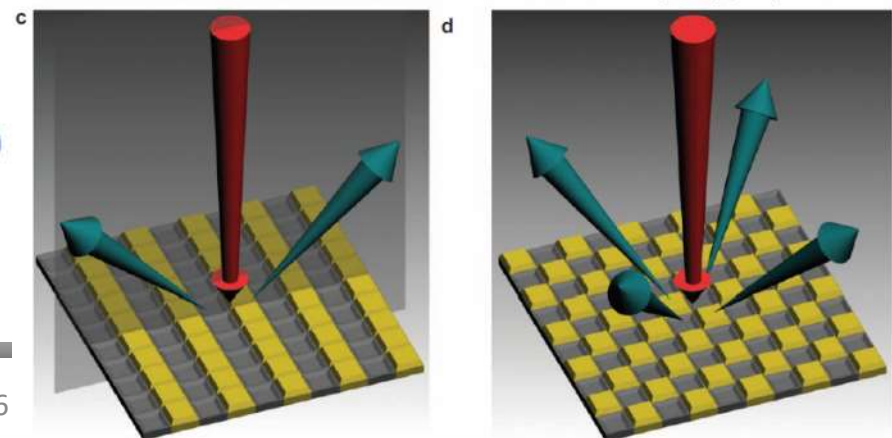
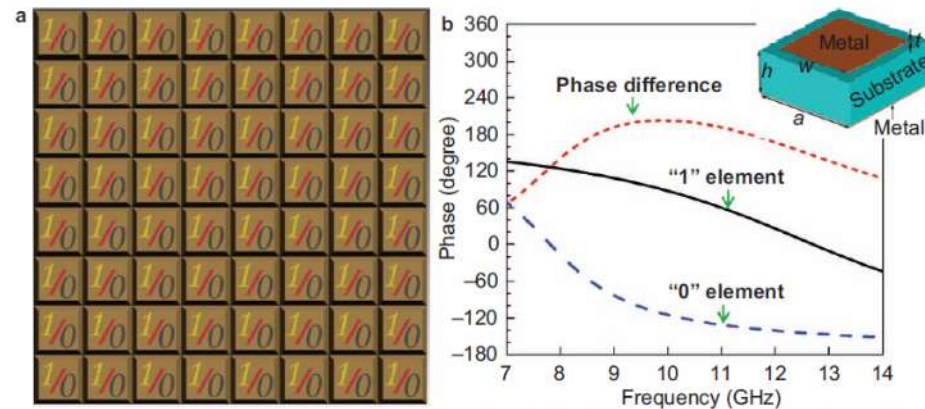
Coding metamaterials, digital metamaterials and programmable metamaterials

Tie Jun Cui^{1,2,*}, Mei Qing Qi^{1,*}, Xiang Wan^{1,*}, Jie Zhao¹ and Qiang Cheng^{1,2}

By coding '0' and '1' elements with controlled sequences (i.e., 1-bit coding), EM waves can be manipulated to realize different functionalities

$$f(\theta, \varphi) = f_e(\theta, \varphi)$$

$$\sum_{m=1}^N \sum_{n=1}^N \exp\{-i\{\varphi(m, n) + kD \sin \theta [(m-1/2) \cos \varphi + (n-1/2) \sin \varphi]\}\} \quad (1)$$



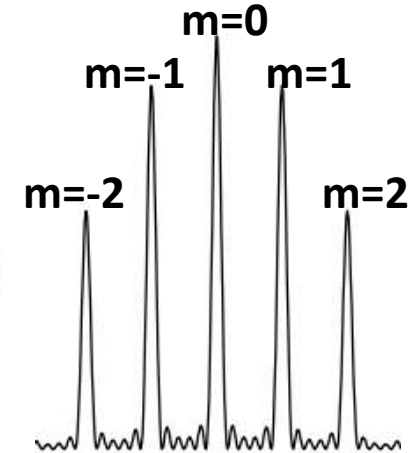
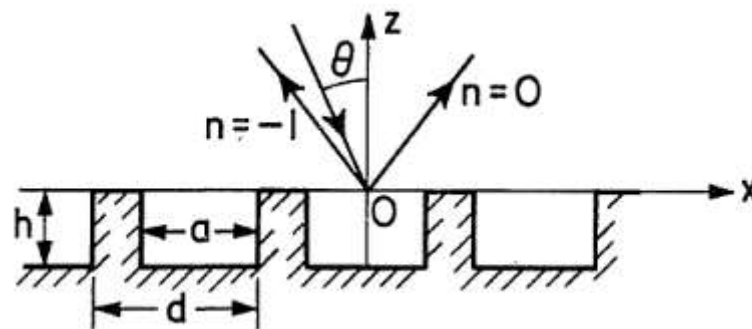
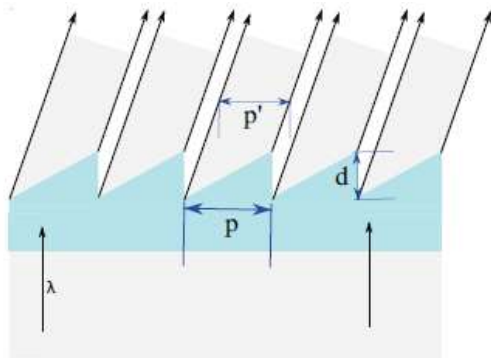
Metagratings

Diffraction grating:

- periodic optical structure with infinite extent in one direction, which is able to diffract light incident on its surface¹

Blazed (echelette) grating:

- capable of scattering an incident wave into a specific diffraction order²



¹M. Born, E. Wolf, "Principles of Optics," chap. Element of the theory of diffraction, pp. 412–516.

²E. V. Jull et al., "Gratings that diffract all incident energy," J. Opt. Soc. Am. **67**(4), 557 (1977).



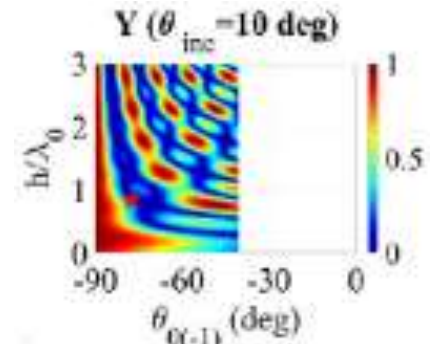
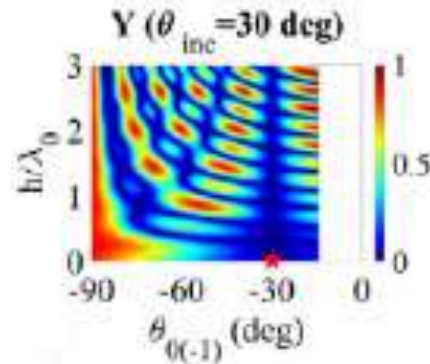
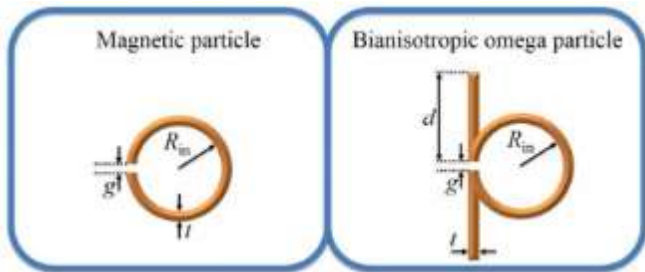
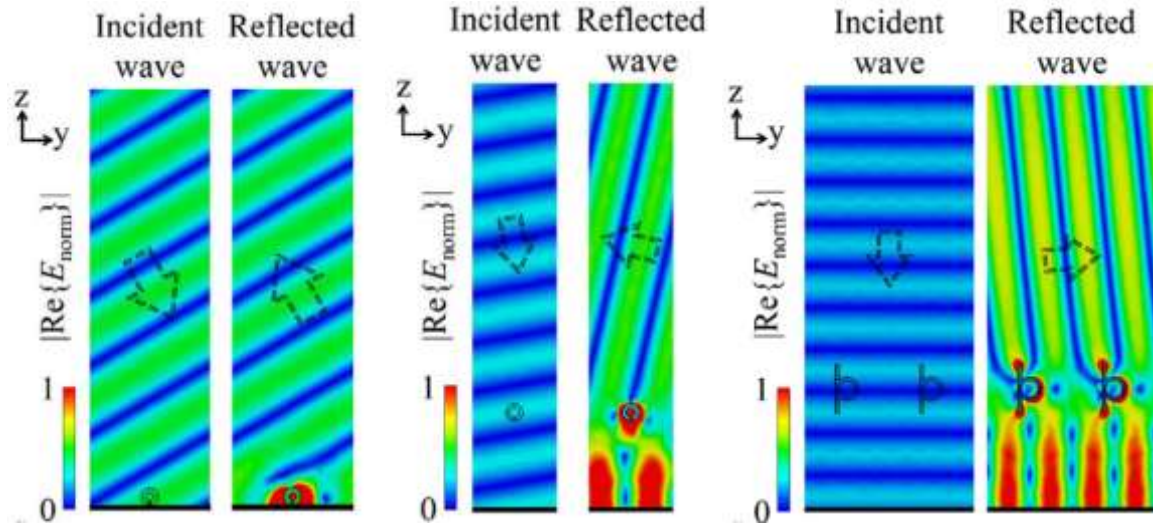
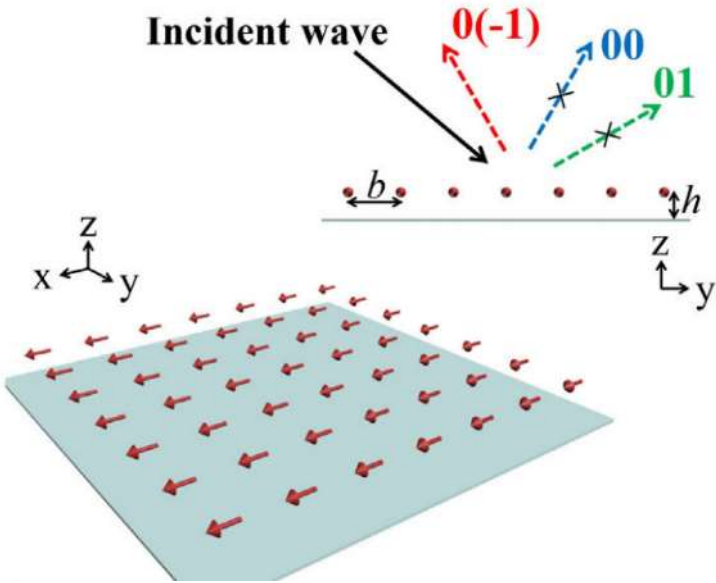
Metagratings: Beyond the Limits of Graded Metasurfaces for Wave Front Control

Younes Ra'di, Dimitrios L. Sounas, and Andrea Alù*

Department of Electrical and Computer Engineering, The University of Texas at Austin, Austin, Texas 78712, USA

- Metasurfaces: limitations in terms of efficiency and fabrication, in particular for extreme manipulation
- 1D gratings: profile modulation in one direction, a translational symmetry in the other and no control of energy in the orders
- Metagratings:
 - evolution of 1D diffraction gratings (construction from meta-atoms whose scattering properties can be judiciously engineered)
 - translation-invariant direction is engineered at a scale $< \lambda$
 - definition of an averaged macroscopic quantity (impedance density)

Metagratings



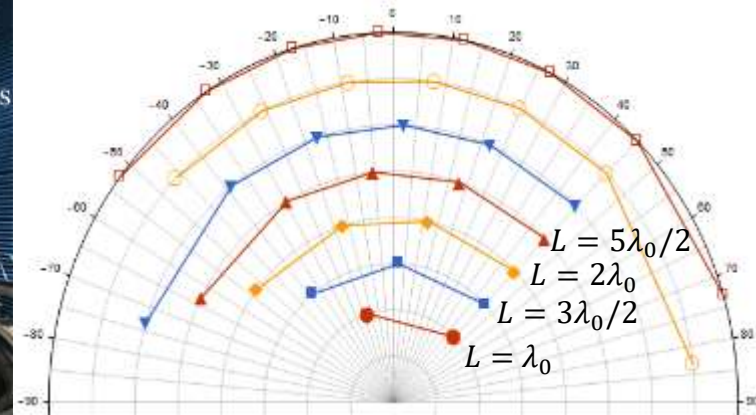
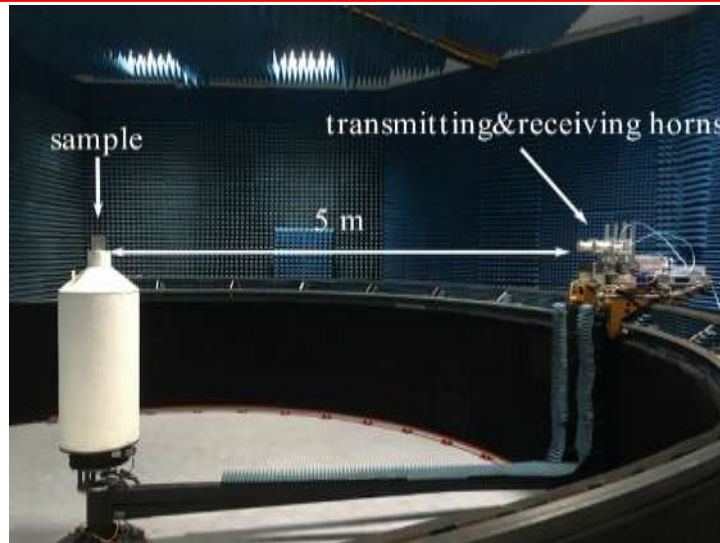
Metagratings

PHYSICAL REVIEW APPLIED 11, 024074 (2019)

Constructing the Near field and Far field with Reactive Metagratings: Study on the Degrees of Freedom

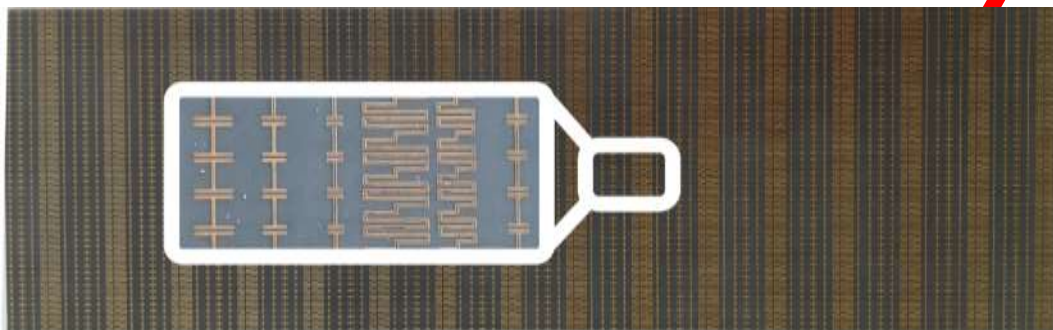
Vladislav Popov,^{1,*} Fabrice Boust,^{1,2} and Shah Nawaz Burokur³

Periodic structures



Plane-wave illumination

Only discrete angles are accessible



Metagratings

The diffraction problem can be solved exactly:

$$E_x^{ref}(y, z < -h) = \sum_{m=-\infty}^{+\infty} A_m^{TE} e^{-j\xi_m y + j\beta_m z}$$

$$A_m^{TE} = -\frac{k\eta \rho_m^{(I)} (1 + R_m^{TE}) e^{j\beta_m h}}{2L \beta_m} + \delta_{m0} R_0^{TE} e^{2j\beta_0 h}$$

$$I_q = \frac{1}{N} \sum_{m=-l}^r \rho_m^{(I)} \exp[-j\xi_m (q-1)d]$$

Load impedance densities Z_q of the line currents I_q are found from:

$$Z_q I_q = E_x^{(exc)}(y_{0q}, -h) - Z_{in} I_q - \sum_{p=1}^N Z_{qp}^{(m)} I_p$$

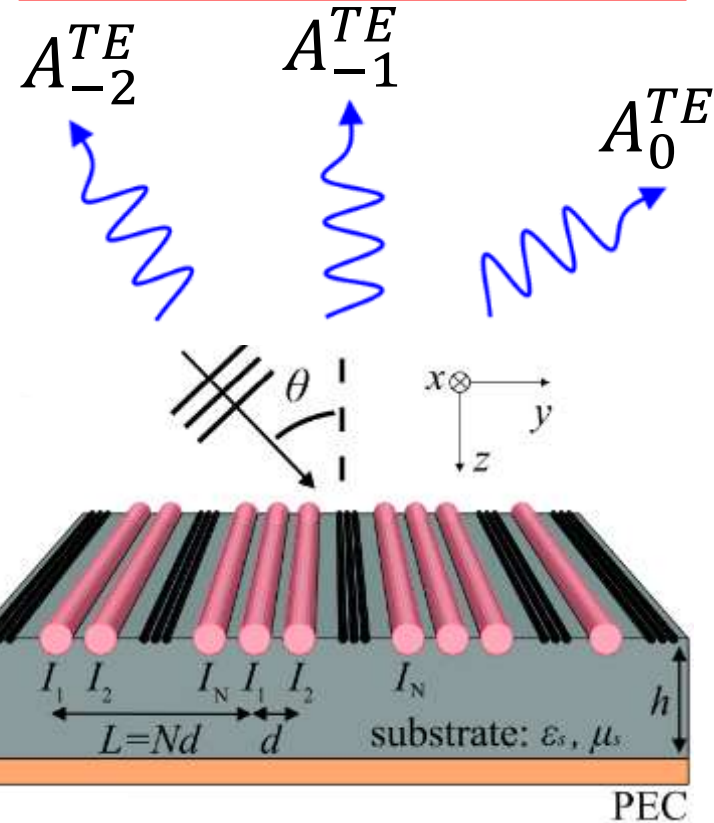
Excitation field

Input impedance

Mutual impedance

diffraction angles :

$$L(\sin[\theta_m] - \sin[\theta_i]) = m\lambda$$

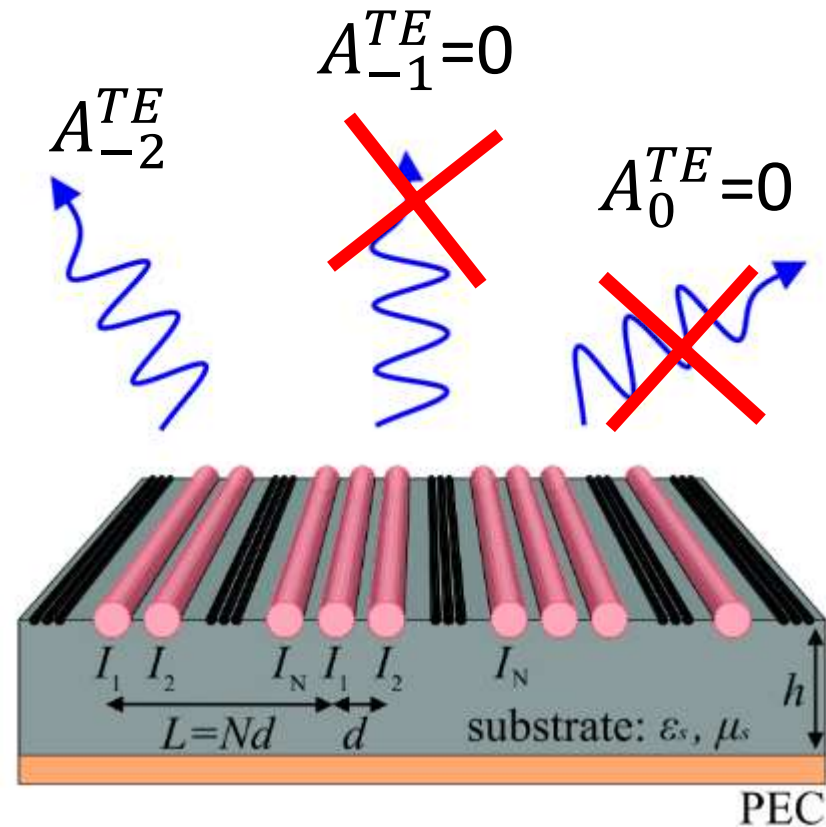


Metagratings

In order to deal only with loads $\Re[Z_q] = 0$ the following equation has to be satisfied:

$$\Re \left[E_x^{(exc)}(y_{0q}, -h) I_q^* - \sum_{p=1}^N Z_{qp}^{(m)} I_p I_q^* \right] = \Re[Z_{in}] |I_q|^2$$

- It is a set of N second order algebraic equations
- When $N = M$, it is impossible to satisfy both equations in general
- Scattering losses appear

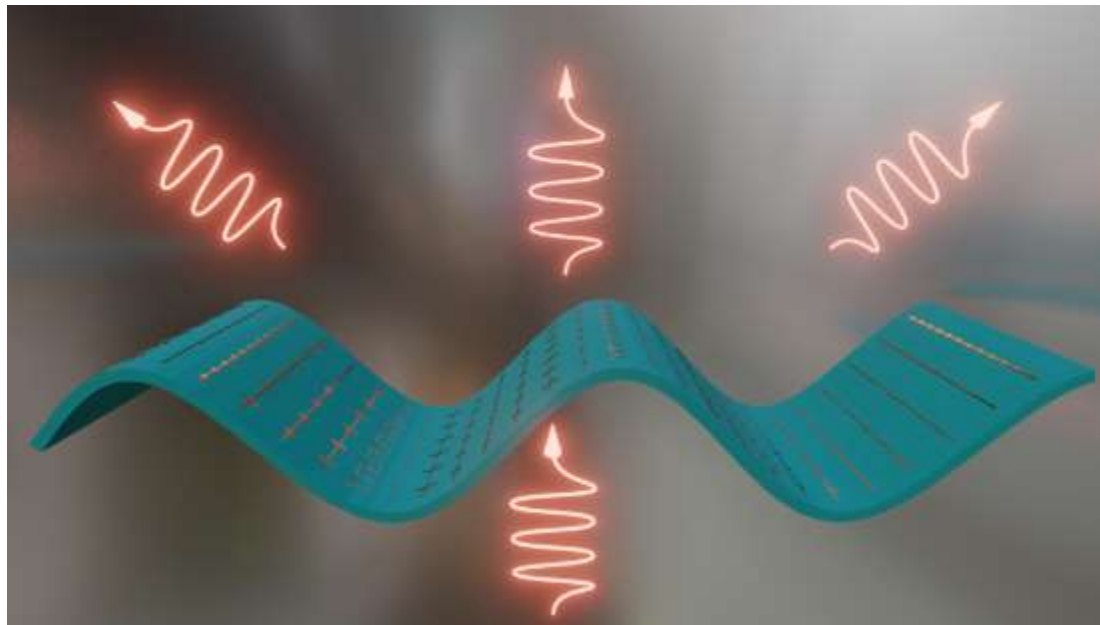


Sparse Metasurfaces

PHYSICAL REVIEW APPLIED 14, 044007 (2020)

Conformal Sparse Metasurfaces for Wavefront Manipulation

Vladislav Popov^{1,*}, Shah Nawaz Burokur^{2,1} and Fabrice Boust^{1,3}



- N loaded wires are distributed along the surface of an arbitrarily-shaped substrate
- The structure is illuminated by an arbitrary wave

Sparse Metasurfaces

Scattering problem

The total field can be written as follows:

$$E_x(\mathbf{r}) = E_x^{(exc)}(\mathbf{r}) + E_x^{(sct)}(\mathbf{r})$$

$$E_x^{(sct)}(\mathbf{r}) = \int G_{xx}(\mathbf{r}, \mathbf{r}') J_x(\mathbf{r}') d\mathbf{r}'$$

Model of infinitely thin wires:

$$J_x(\mathbf{r}) = \sum_{q=1}^N I_q \delta(\mathbf{r} - \mathbf{r}_q)$$

$$E_x(\mathbf{r}) = E_x^{(exc)}(\mathbf{r}) + \sum_{q=1}^N G_{xx}(\mathbf{r}, \mathbf{r}_q) I_q$$

Ohm's law:

$$Z_q I_q = E_x^{(ext)}(\mathbf{r}_q) - \sum_{p=1}^N Z_{qp}^{(m)} I_p$$

Mutual-impedance densities

Sparse Metasurfaces

Green's function

A Green's function is defined as:

$$\left(\frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} + \varepsilon_r(\mathbf{r})k_0^2 \right) G_{xx}(\mathbf{r}, \mathbf{r}') = j\omega\mu_0\delta(\mathbf{r} - \mathbf{r}')$$

Mutual-impedance densities are calculated as:

$$Z_{qp}^{(m)} = -G_{xx}(\mathbf{r}_q, \mathbf{r}_p), q \neq p,$$

$$Z_{qq}^{(m)} = -\frac{1}{2\pi r_{eff}} \oint G_{xx}(\mathbf{r}, \mathbf{r}_q) d\mathbf{r}.$$

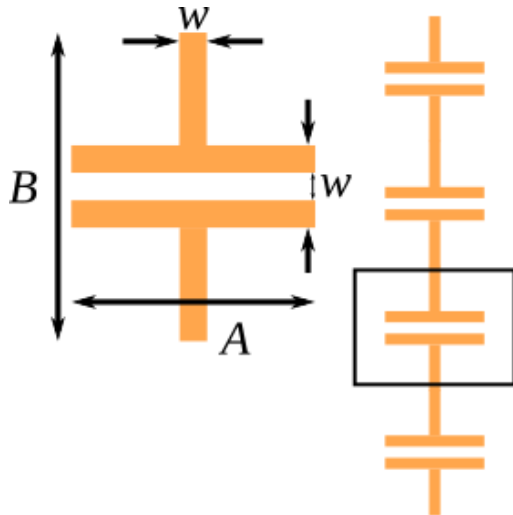
A Green's function can be calculated numerically by means of full-wave simulations

Sparse Metasurfaces

Implementation of loaded wires

$$\text{Im}[Z_L] < 0$$

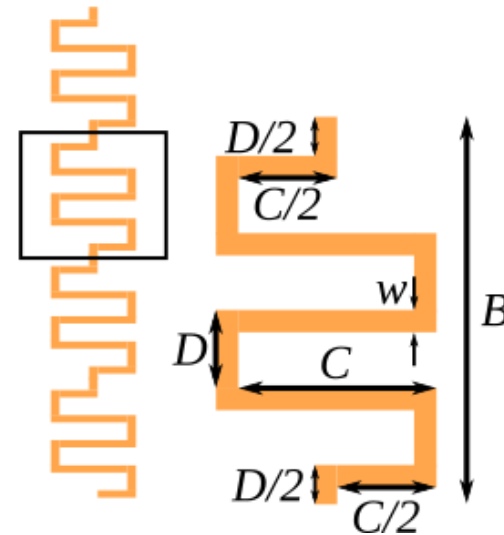
Printed capacitor



Change the **gap** to engineer the capacitive response

$$\text{Im}[Z_L] > 0$$

Printed inductor



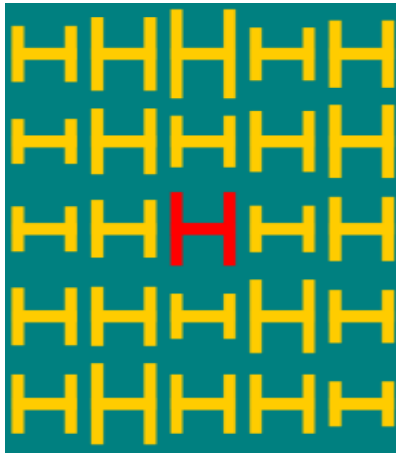
Change the effective **length** to engineer the inductive response

Sparse Metasurfaces

Designing **sparse** Metasurfaces

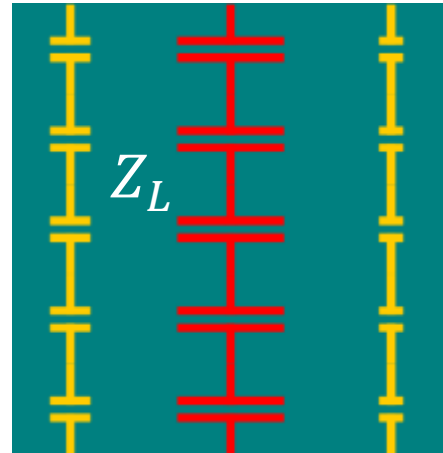
LPA of **dense** metasurfaces cannot be used for **sparse** ones

Dense Metasurface
Non-uniform array

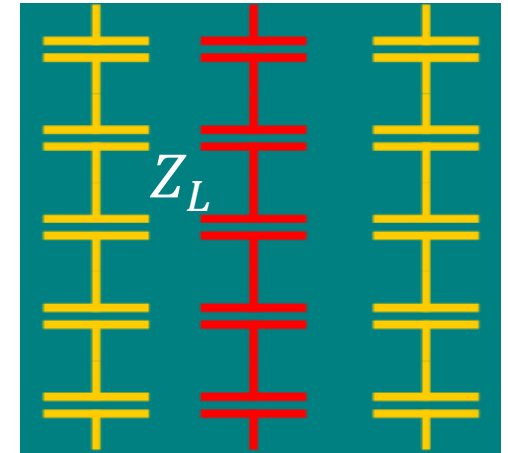


Sparse Metasurface

Non-uniform array



Uniform array



Sparse Metasurfaces

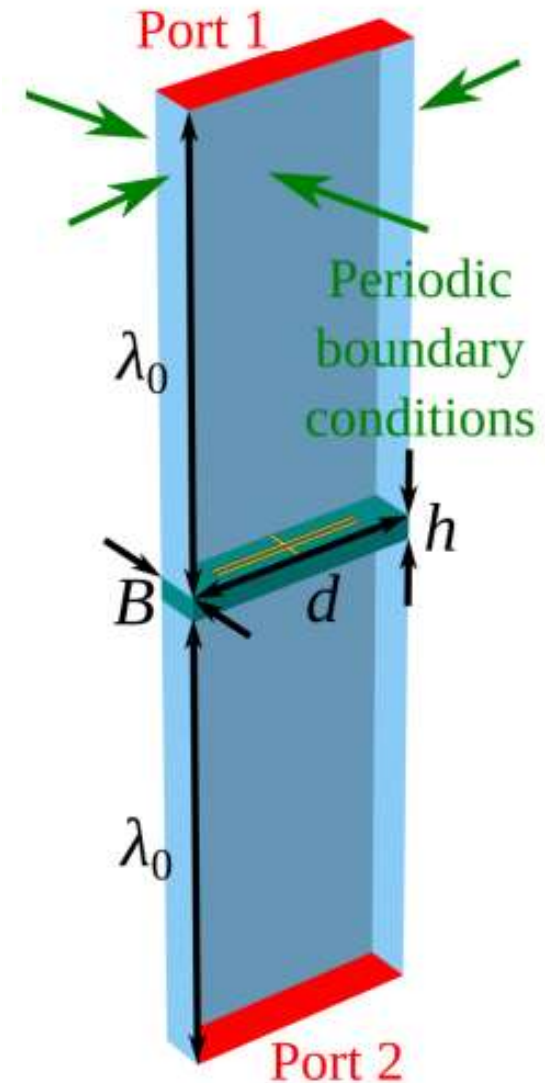
Load-impedance density engineering

- 3D full-wave simulations are used to calculate A_0^{TE} (S_{11} scattering parameter) for a uniform array of loaded wires
- After that, analytical formulas are used to retrieve load-impedance density

$$\square I = -\frac{2d\beta_0}{k\eta} \frac{A_0^{TE} - R_0^{TE} e^{2j\beta_0 h}}{(1 + R_0^{TE}) e^{j\beta_0 h}}$$

$$\square Z_q I = E_0 - \frac{k\eta}{4} I H_0^{(2)}(k_0 r_{eff}) - Z_m I$$

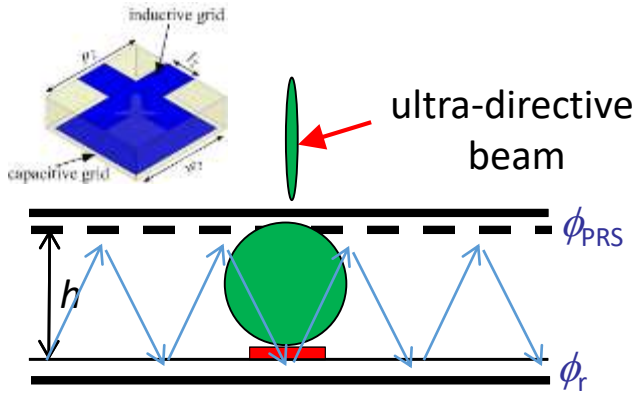
$$\square E_0 = (1 + R_0^{TE}) e^{j\beta_0 h}$$



3. Metasurface applications

- Antennas
- Lenses
- Absorbers
- Polarization converters
- Wavefront engineering

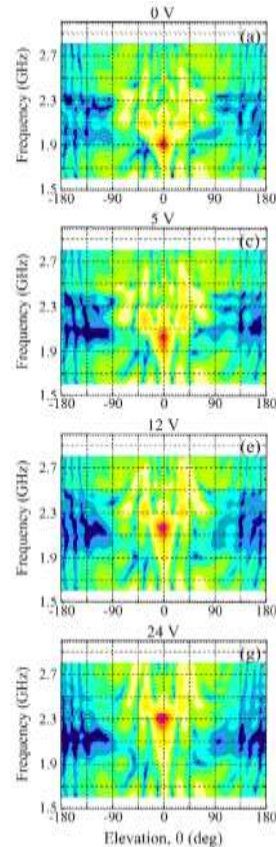
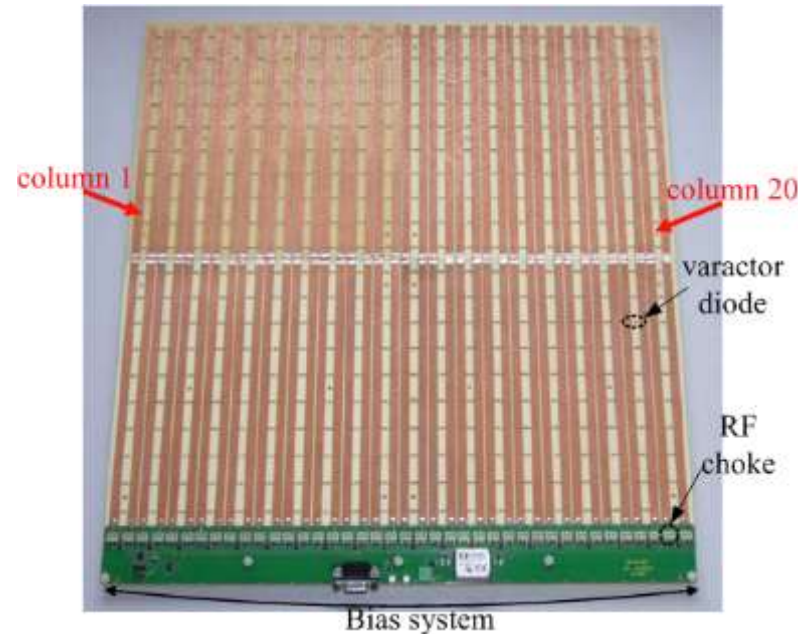
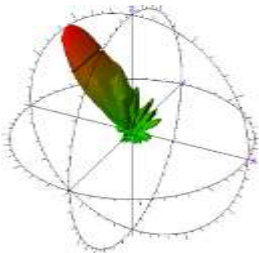
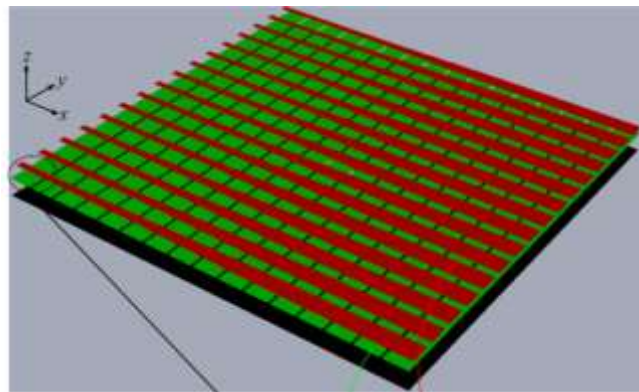
3. Metasurface applications: antennas



Thickness h of the cavity at resonance:

$$h = \frac{\lambda}{4\pi} (\phi_{\text{PRS}} + \phi_r) \pm N \frac{\lambda}{2}$$

We minimize $(\phi_{\text{PRS}} + \phi_r)$ to reduce $h \rightarrow$ **Metasurface**¹

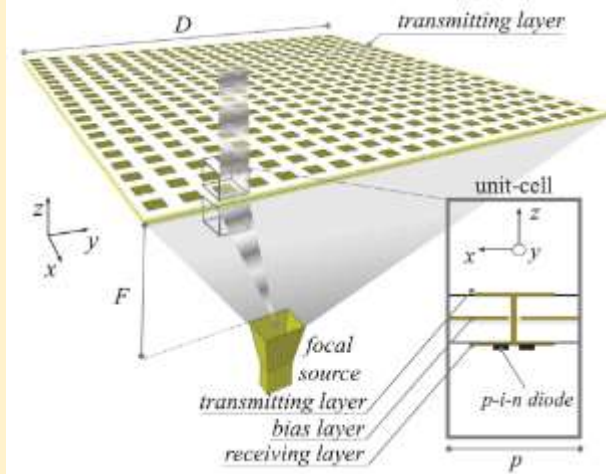


¹S. N. Burokur et al., Metasurfaces for high directivity antenna applications in book Metamaterial, ISBN 978-953-51-0591-6, InTech.

3. Metasurface applications: antennas

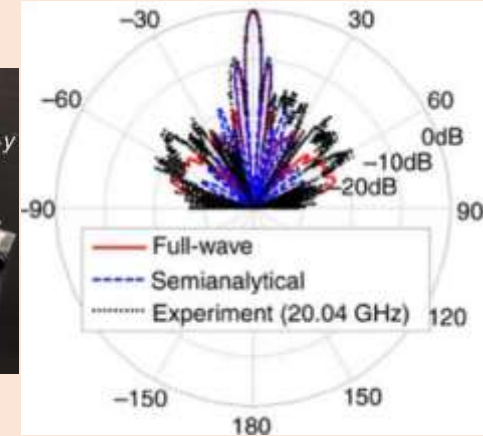
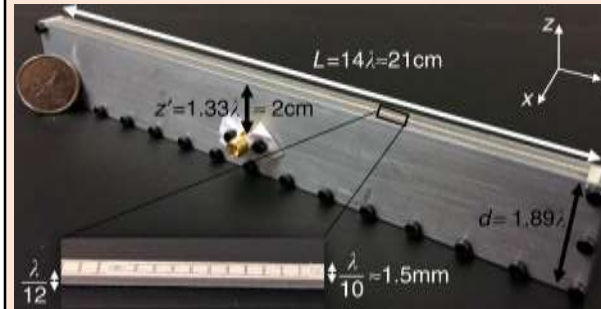
Transmit-array antenna

L. Di Palma et al., IEEE TAP **65**(2), 529(2017)



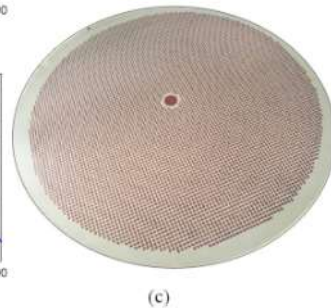
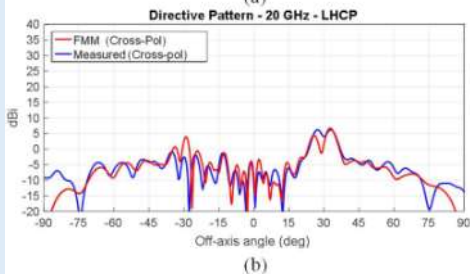
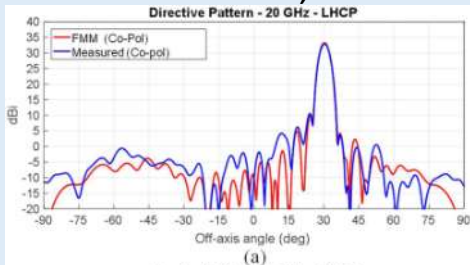
Cavity-excited Huygens' metasurface antenna

A. Epstein et al., Nat. Commun. **7**, 10360(2016)



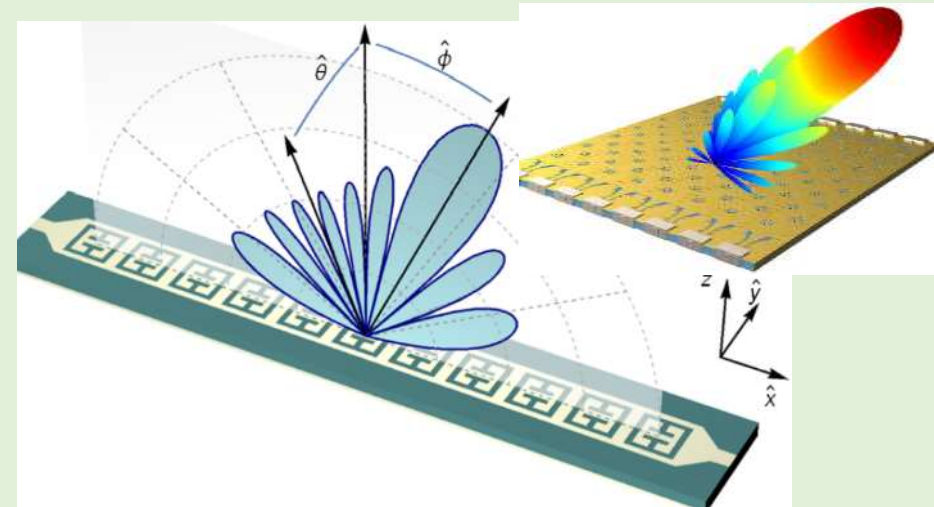
Modulated metasurface antenna

G. Minatti et al., IEEE TAP **65**(4), 1532(2017)



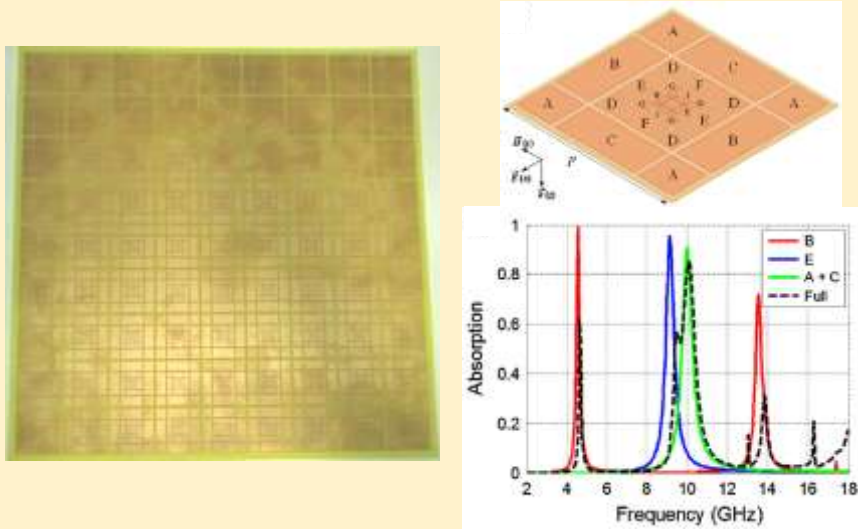
Waveguide-fed metasurface antenna

D. R. Smith et al., Phys. Rev. Appl. **8**, 054048 (2017)

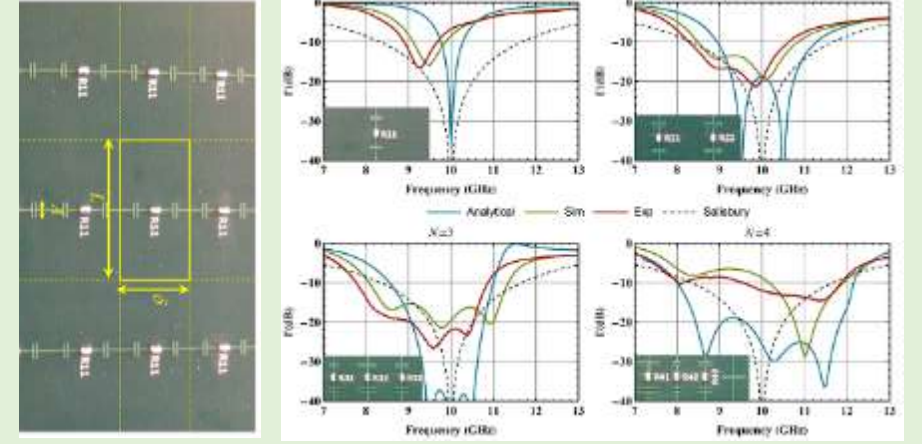


3. Metasurface applications: absorbers

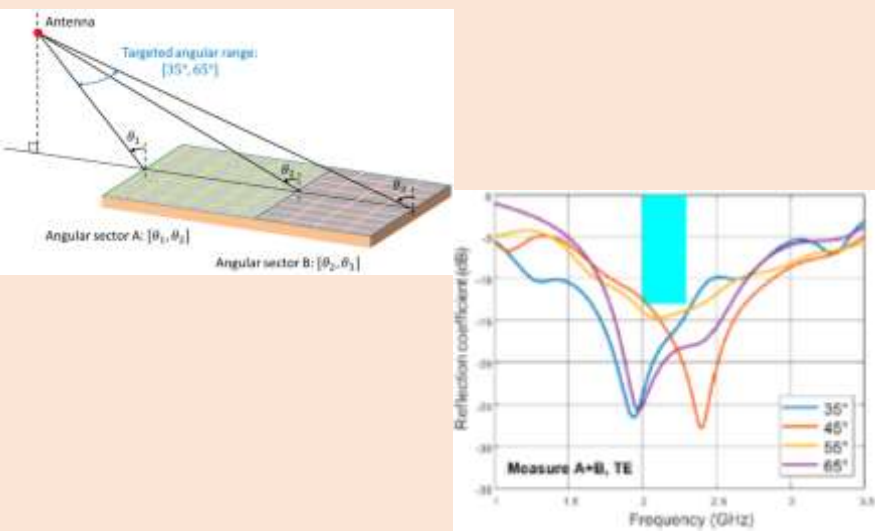
A. Sellier et al., Appl. Phys. A **117**, 739(2014)



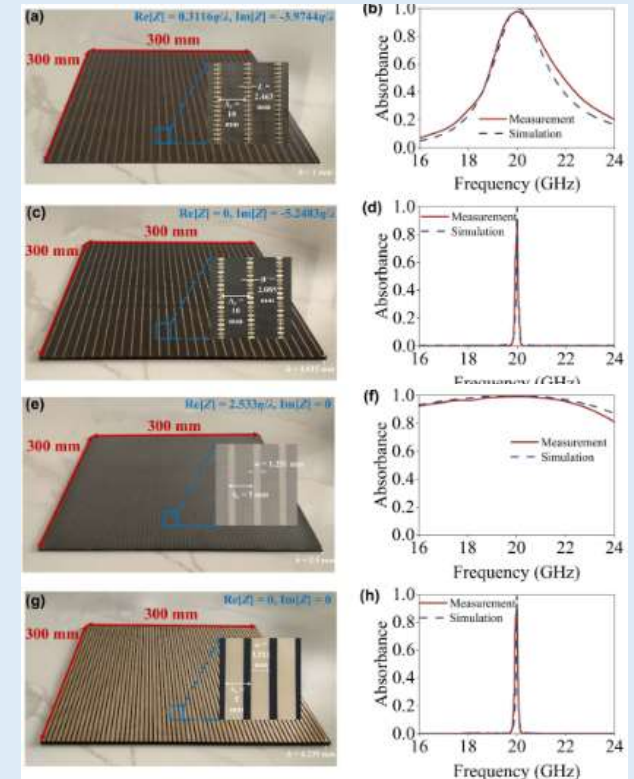
F. Boust et al. Opt. Lett. **47**, 5305(2022)



O. Rance et al., Appl. Sci. **9**(16), 3425(2019)



Z. Tan et al., IEEE TAP **71**, 1832(2023)



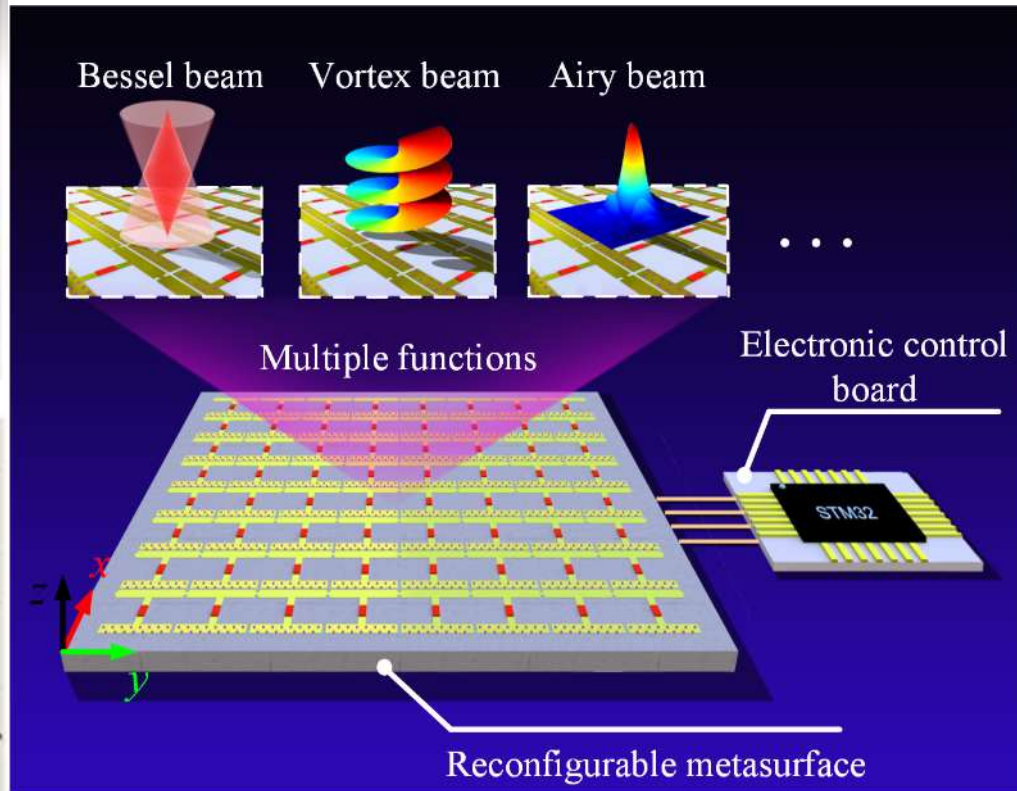
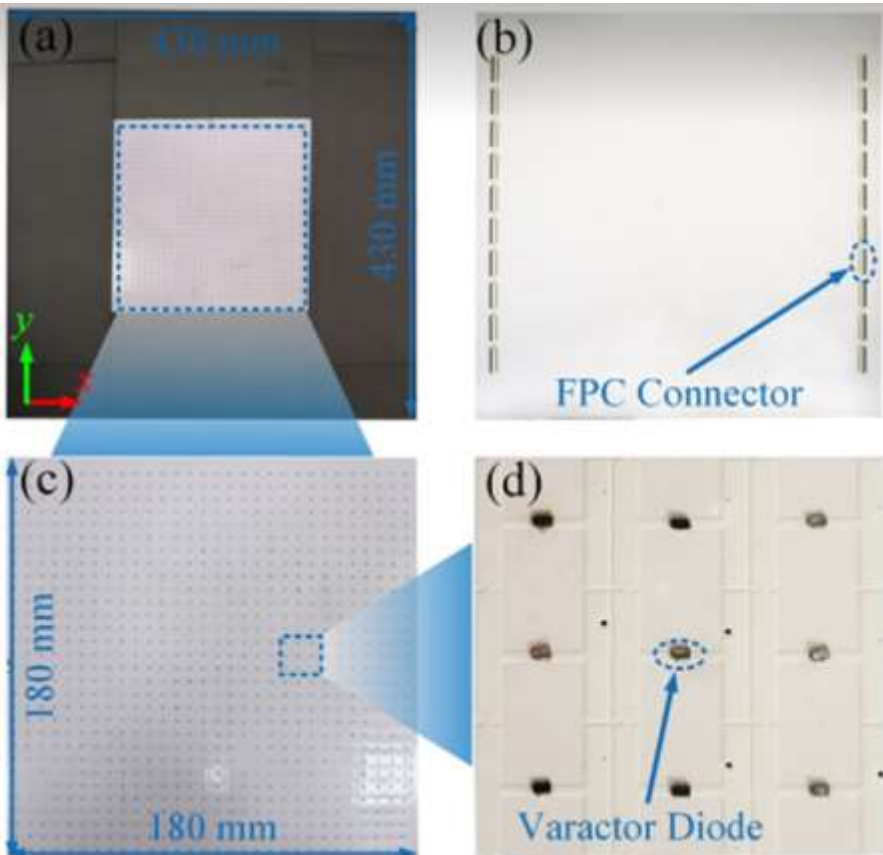
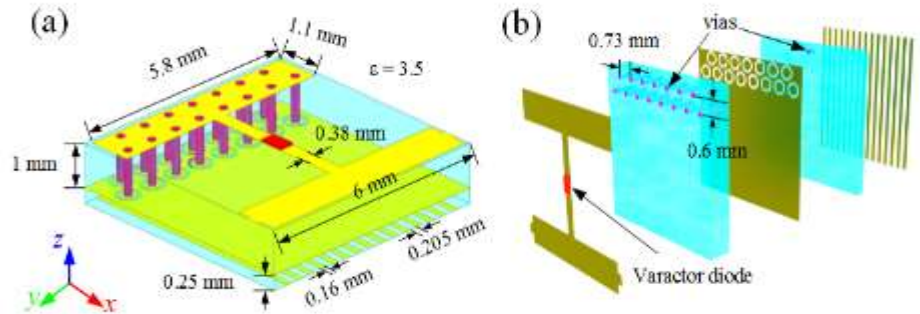
3. Metasurface applications: complex waves

1650 Vol. 9, No. 9 / September 2021 / Photonics Research Research Article

PHOTONICS Research

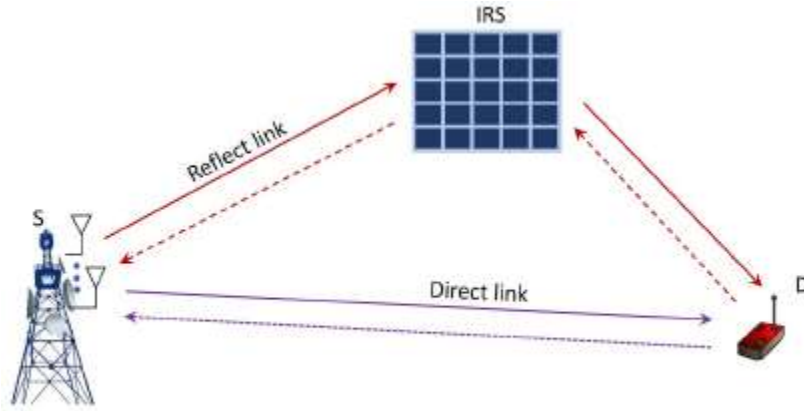
Versatile metasurface platform for electromagnetic wave tailoring

RUI FENG,^{1,2} BADREDDINE RATNI,² JIANJIA YI,^{1,2} HAILIN ZHANG,¹ ANDRÉ DE LUSTRAC,^{2,5} AND SHAH NAWAZ BUROKUR^{3,*}



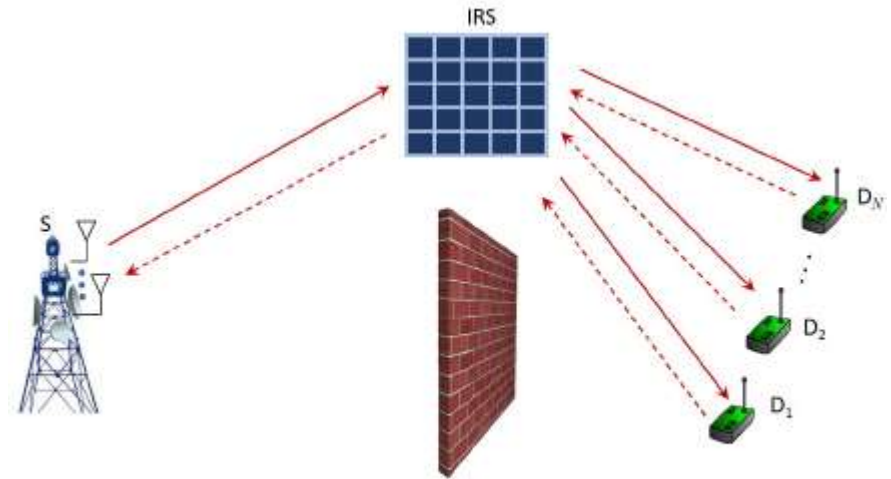
3. Metasurface applications: RIS

FD transmission: diversity gains to improve the received SNR at D and S



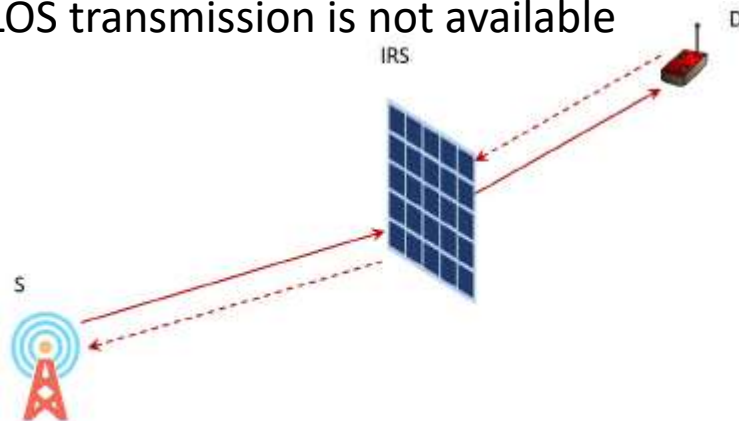
(a) LOS scenarios

FD transmission: communicating with multiple terminals through reflection



(b) NLOS scenarios with reflect waves

FD transmission: S and D located at each side of a RIS and LOS transmission is not available



(c) NLOS scenarios with transmission waves

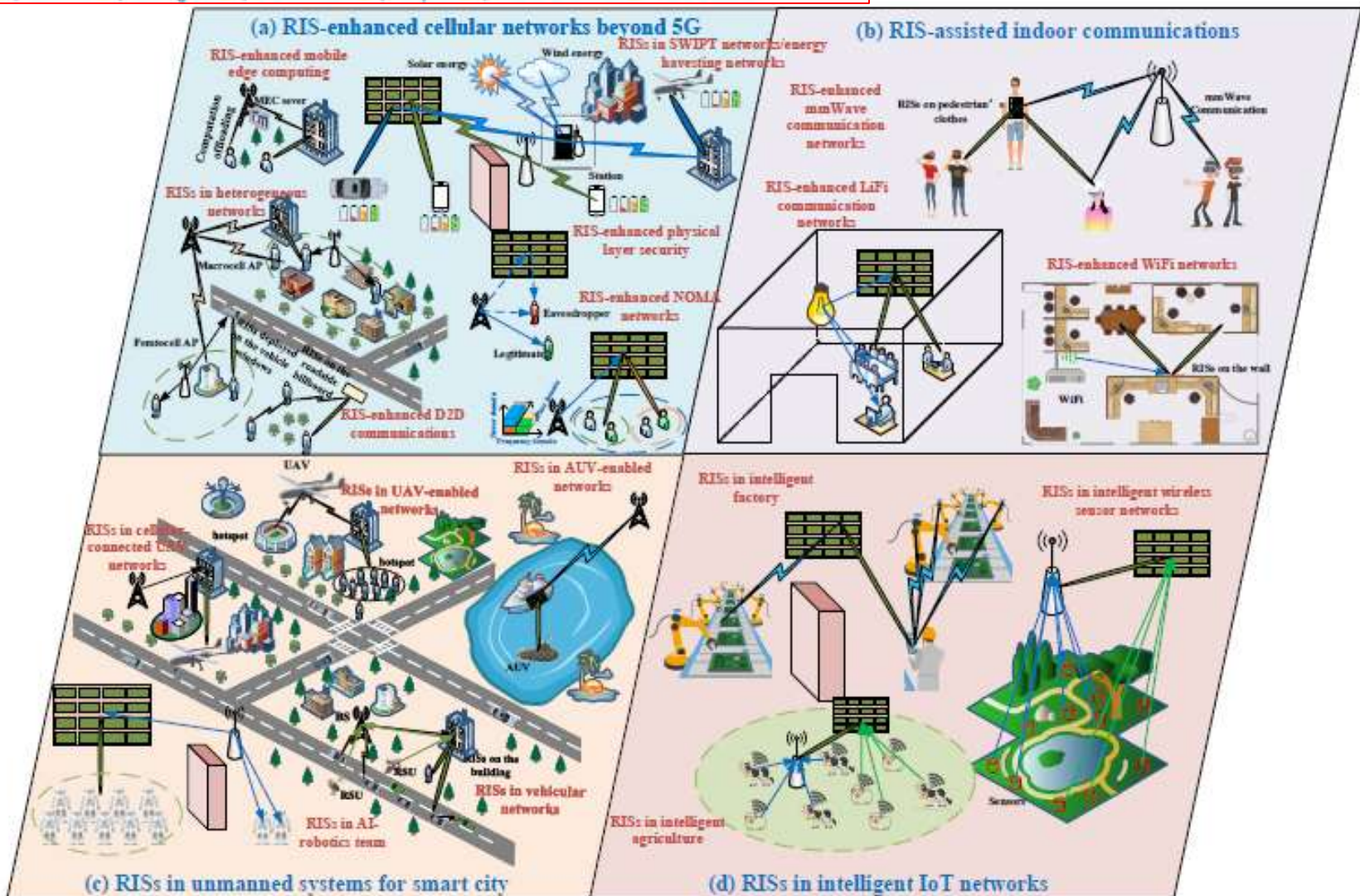
3. Metasurface applications: RIS

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Reconfigurable Intelligent Surfaces: Principles and Opportunities

Publisher: IEEE Cite This PDF

Yuanwei Liu; Xiao Liu; Xidong Mu; Tianwei Hou; Jiaqi Xu; Marco Di Renzo All Authors



3. Metasurface applications: RIS

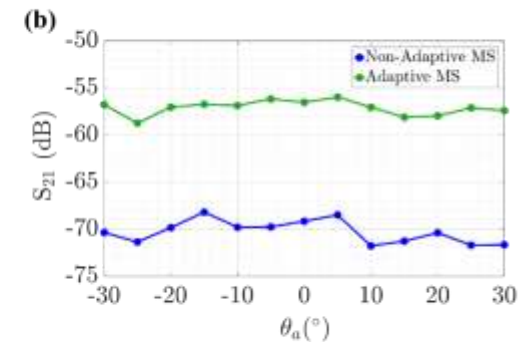
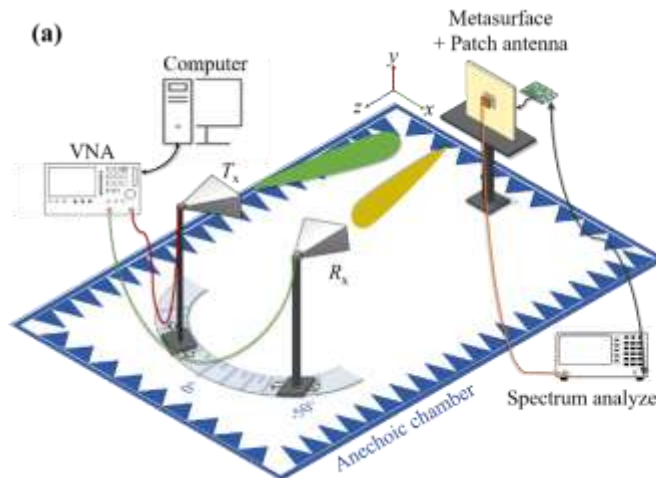
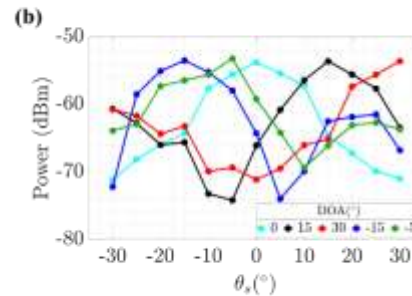
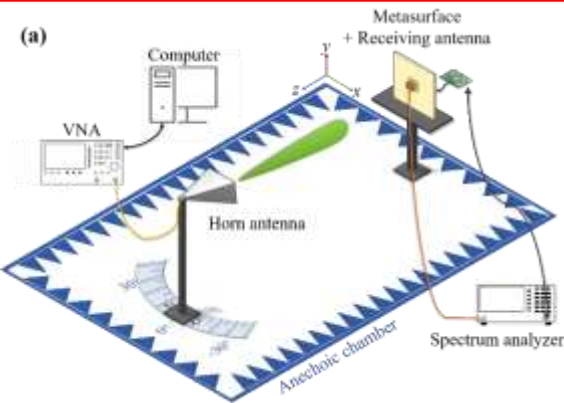
ADVANCED MATERIALS TECHNOLOGIES

Research Article

Programmable Meta-Reflector for Multiple Tasks in Intelligent Connected Environments

Nawel Meftah, Badreddine Ratni, Mohammed Nabil El Korso, Shah Nawaz Burokur

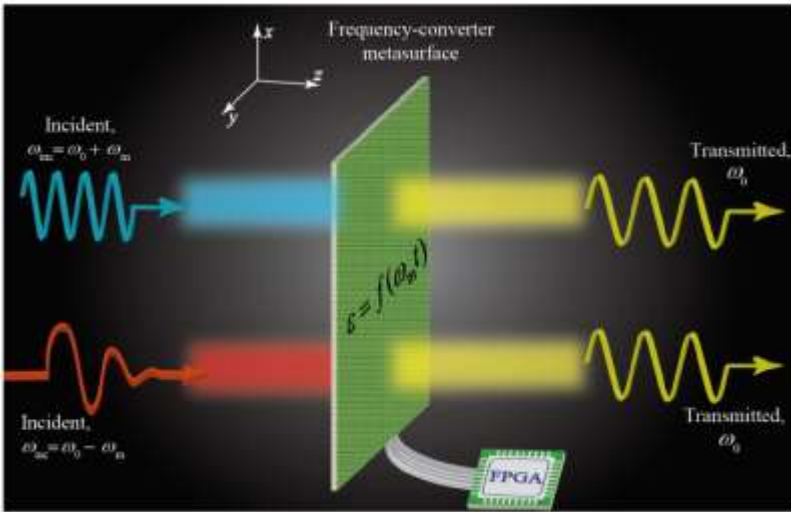
First published: 08 April 2024 | <https://doi.org/10.1002/admt.202400006>



4. Actual trends: Temporal modulation

Pure and Linear Frequency-Conversion Temporal Metasurface

Sajjad Taravat and George V. Eleftheriades
 Phys. Rev. Applied **15**, 064011 – Published 4 June 2021

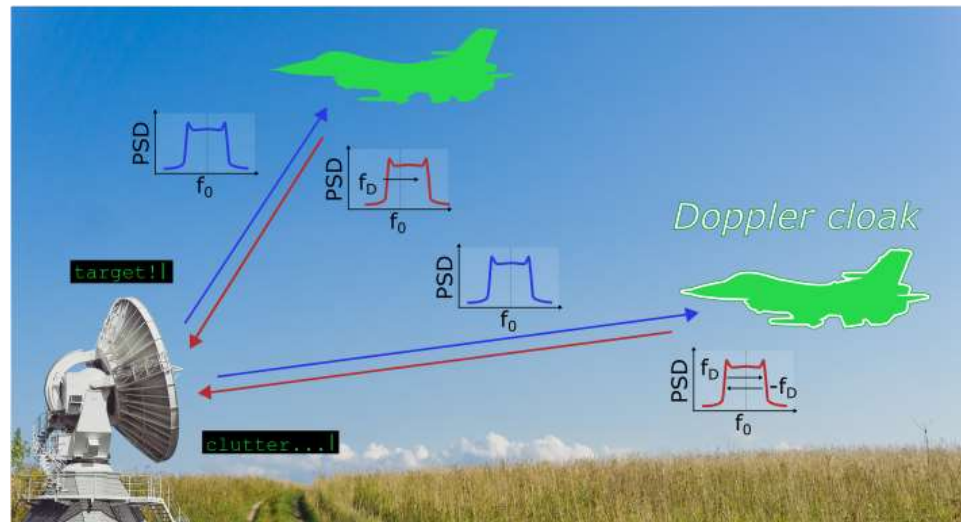


- Transition from the fundamental temporal frequency ω_0 to an infinite number of time frequency harmonics $\omega_0 \pm n\omega_m$.
- Hence, the output wave includes time harmonics of the modulation wave

Tanguy Lopez

Metasurface-based radar stealth solutions over VHF-UHF bands: Tunable absorption and Doppler cloaking

Thèse présentée et soutenue publiquement le 09/10/2024



4. Actual trends: Temporal modulation

Research Square
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Article
Simplified radar architecture based on information metasurface

Tie Jun Cui, Si Ran Wang, Zhan Ye Chen, Shao Nan Chen, Jun Yan Dai, and 8 more

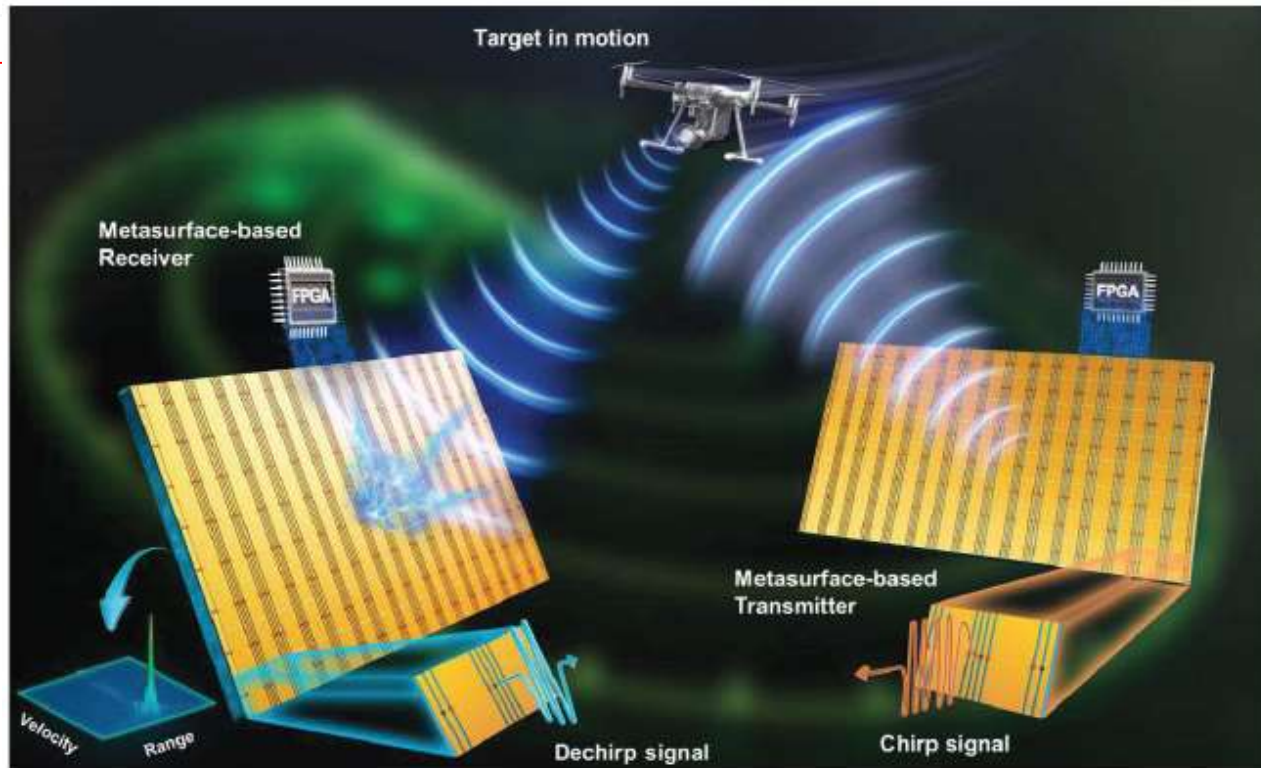
This is a preprint; it has not been peer reviewed by a journal.

At transmitting end:

- Beamforming
- radar-signal generation (no active RF devices)

At receiving end:

- capturing the echo waves
- transforming the broadband chirp signals into narrowband signals (avoiding the conventional RF hardware), lowering prohibitively high AD sampling rates



4. Actual trends: Mathematical operations



ARTICLE

<https://doi.org/10.1038/s41467-022-29732-4>

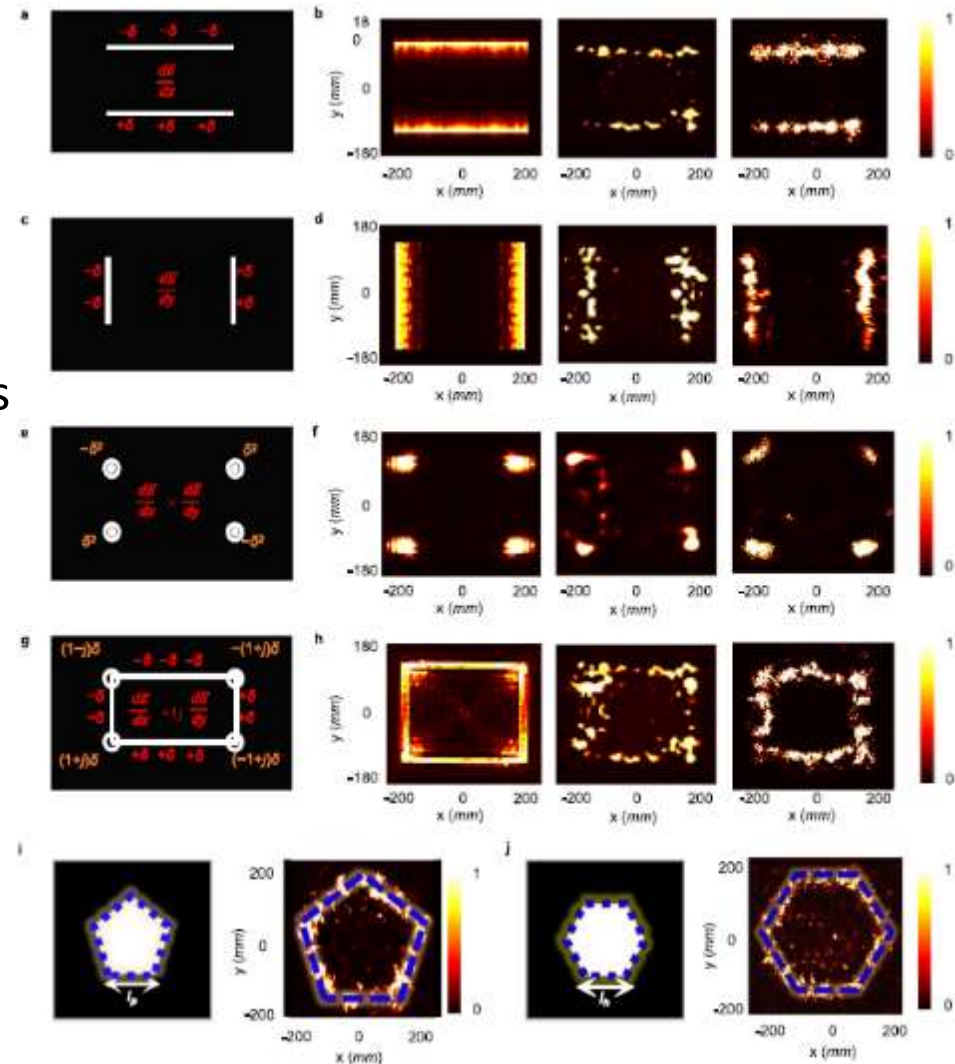
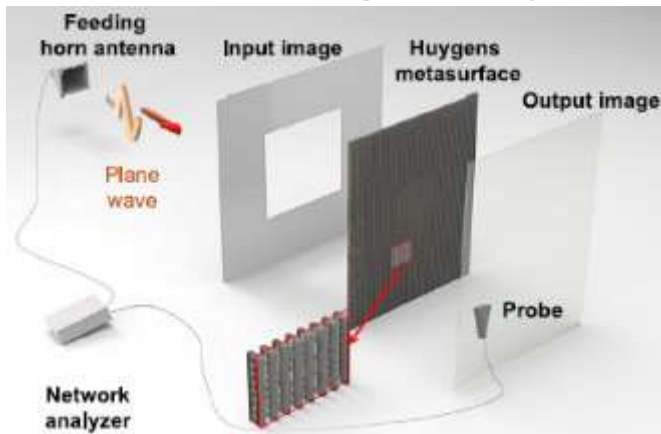
OPEN

Check for updates

Single-layer spatial analog meta-processor for imaging processing

Zhuochao Wang^{1,6}, Guangwei Hu^{2,8}, Xinwei Wang^{1,6}, Xumin Ding^{1,3,4,5}, Kuang Zhang^{6,8}, Haoyu Li^{1,4}, Shah Nawaz Burakur^{7,8}, Qun Wu⁶, Jian Liu^{1,3,4,5}, Jiubin Tan^{1,3} & Cheng-Wei Qiu^{2,8}

- performing analog optical computations based on Fourier transform
- Edge detection operation: dramatic change of the derivatives of signals due to the sudden change of objects



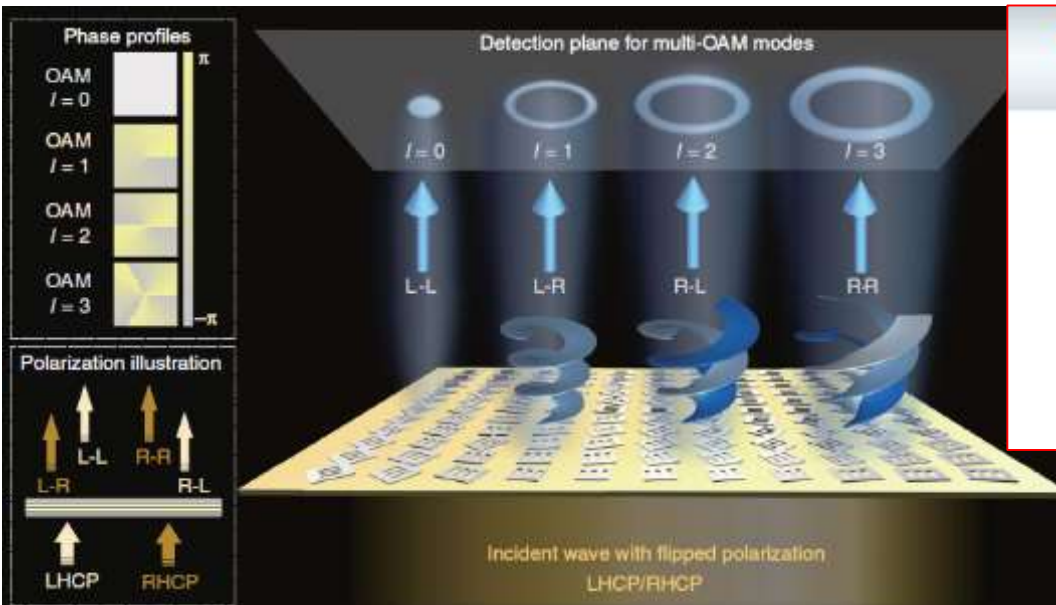
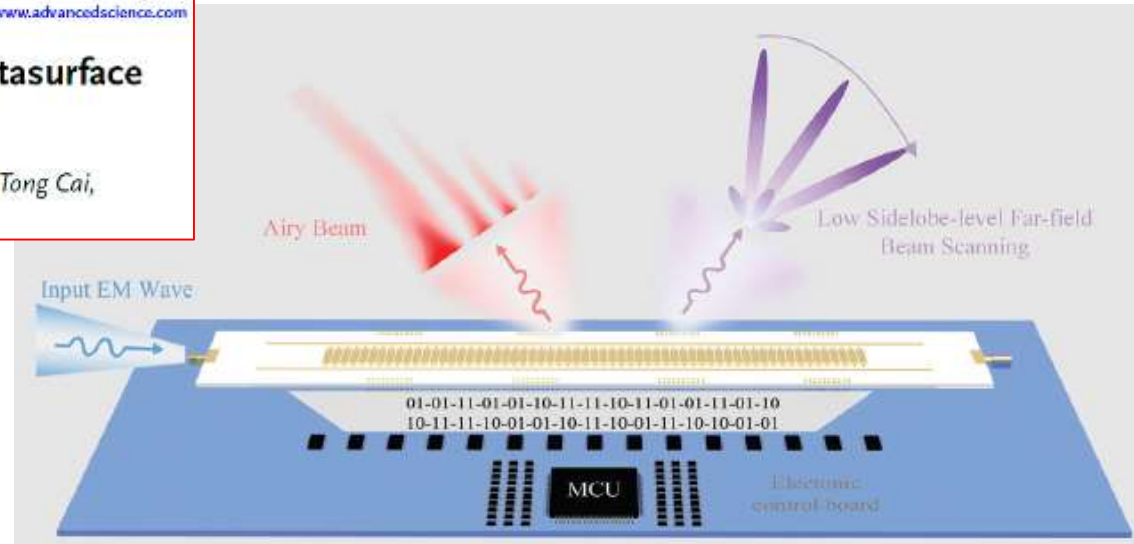
4. Actual trends: Multiplexing

RESEARCH ARTICLE

ADVANCED SCIENCE
www.advancedscience.com

Complex-Amplitude Programmable Versatile Metasurface Platform Driven by Guided Wave

Jian-Qiao Han, Fan-Yi Meng,* Chunsheng Guan,* Cong Wang, Tao Jin, Tong Cai, Chang Ding,* Shah Nawaz Burokur, Qun Wu, and Xumin Ding*



nature COMMUNICATIONS

ARTICLE

<https://doi.org/10.1038/s41467-020-17773-4> OPEN

Independent phase modulation for quadruplex polarization channels enabled by chirality-assisted geometric-phase metasurfaces

Yueyi Yuan¹, Kuang Zhang¹, Badreddine Ratni², Qinghua Song³, Xumin Ding^{1,4,5*}, Qun Wu¹, Shah Nawaz Burokur^{2,6*} & Patrice Genevet^{3,4*}

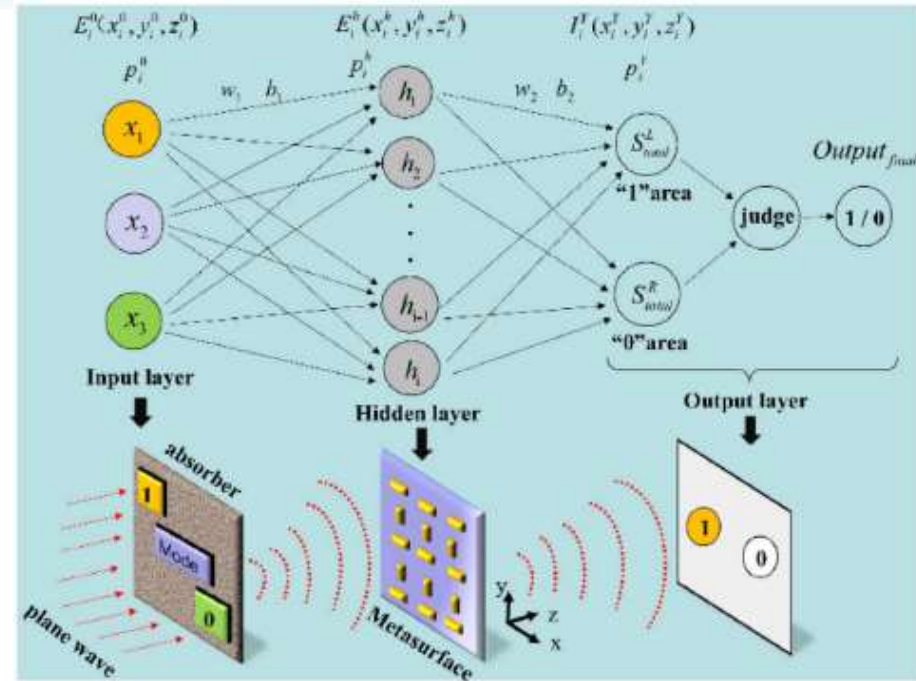
4. Actual trends: Learning-based metasurfaces

318 Vol. 10, No. 2 / February 2022 / Photonics Research **Research Article**

PHOTONICS Research

Compact logic operator utilizing a single-layer metasurface

ZIHAN ZHAO,^{1,2,†} YUE WANG,^{1,†} XUMIN DING,^{1,4} HAoyu LI,^{1,5} JIAHUI FU,² KUANG ZHANG,^{2,6} SHAH NAWAZ BUROKUR,^{3,7} AND QUN WU²

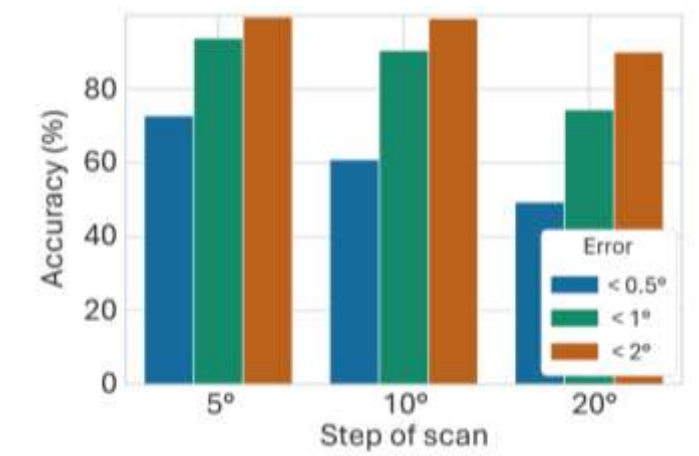
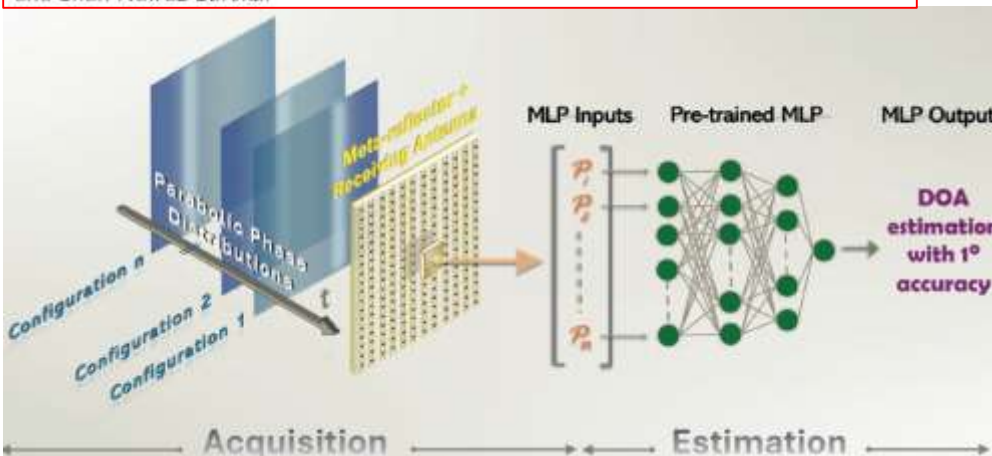


RESEARCH ARTICLE

ADVANCED ELECTRONIC MATERIALS
www.advelectronicmat.de

Enhanced-Resolution Learning-Based Direction of Arrival Estimation by Programmable Metasurface

Nawel Meftah, Badreddine Ratni, Mohammed Nabil El Korso,* and Shah Nawaz Burokur*



5. Summary

- Various designs
- Various technologies/process
- Revisiting traditional architectures
- Novel designs with additional degrees of freedom
- Performances of metasurfaces v/s traditional devices ???

Thanks for your attention!